

Mine Ventilation

→ NVP (Natural Ventilating Pressure)

$$\rightarrow D(\rho_d - \rho_u)g$$
$$\rightarrow \frac{DgB}{287.1} \left[\frac{T_u - T_d}{T_u \times T_d} \right] \times 10^3 \text{ Pa}$$

$T_u \rightarrow$ Temp. of UC shaft (K)

$T_d \rightarrow$ Temp. of DC shaft (K)

$B \rightarrow$ Barometric pressure of UC & DC shaft (kPa)

$D =$ Depth of DC shaft (m)

ρ_d & $\rho_u =$ Air densities of UC & DC shaft

→ Motive column → i) $H = \frac{\rho_d - \rho_u}{\rho_d} \times D$

ii) $\frac{T_u - T_d}{T_u} \times D$

iii) $NVP = H$

$$\rho_{\text{dry air}} = \frac{B \times 10^3}{287.1 T} \text{ kg/m}^3$$

$$\rho_{\text{moist air}} = \left[\frac{B - 0.378e}{287.1 T} \right] \times 10^3 \text{ kg/m}^3$$

$e =$ vap. pressure (kPa)

→ Rate of auxiliary ventilation required to bring down conc. of nitrous fumes to permissible level

$$\phi = 2.3 \cdot \left(\frac{v_{m}}{t} \right) \log \left[\frac{C_0}{C_p} \right] + \left(\frac{v - v_m}{t} \right) \text{ m}^3/\text{min}$$

✓ C_0 → Initial conc. of nitrous fumes (%)

✓ C_p = permissible conc. of nitrous fumes (%)

✓ v = Vol. of working place

✓ v_m = Vol. of mixing zone

✓ $t = \frac{15 \times w \times h}{\text{Safetime}} = 30 \text{ min}$

→ Air power → $P \cdot \phi \times 10^{-3} \text{ kW}$
 \downarrow \downarrow
 Pa m^3/s

$$1 \text{ hp} = 746 \text{ W}$$

$$1 \text{ W} = \frac{1}{746} \text{ hp}$$

→ Critical pressure of booster fan

$$= \frac{P_{fan} \times R_{split \text{ lin}}}{R_{T0}} \text{ which booster fan is (installed)}$$

Conventions

- i) 1 mm wg \rightarrow 9.81 Pa ✓
- ii) 1 mm Hg \rightarrow 133.3 Pa ✓
- iii) 1 Weisbach \rightarrow 9.81 Ns^2m^{-8} ✓
- iv) 1 mwg \rightarrow 0.00981 Ns^2m^{-8} ✓

v) R \rightarrow Weisbach
P \rightarrow mm wg

$$0.001 = \frac{0.00981 \times 1000}{1 \times 10^6} \times 9.81$$

Theoretical depression (H)

For Backward bladed fan

$$H = \frac{v^2 - uv \cot \alpha}{g}$$

For Forward Bl. fan $H = \frac{v^2 + uv \cot \alpha}{g}$

For Radial fan $\rightarrow H = \frac{v^2}{g}$

u = Radial velocity of air leaving the fan (flow velocity m/s)

v = Peripheral speed of blade tips (m/s)
 $= \frac{\pi D N}{60}$

α = ext. angle b/w fan blade and tangent at the periphery

Relative Quantity Method

$$P = \frac{k S \phi^2}{A^3} \text{ (Atkinson eq.)}$$

If pressure is same & nature of lining is same

$$\frac{K S \phi_1^2}{A_1^3} = \frac{K S \phi^2}{A^3}$$

$$\phi = \sqrt{\frac{P A^3}{K S}}$$

$$\phi = \sqrt{\frac{A^3}{K S}}$$

Relative quantity in splits (q_1) = $\sqrt{\frac{A_1^3}{L_1 P_1}}$

$$q_2 = \sqrt{\frac{A_2^3}{L_2 P_2}}$$

$$q_1 = \phi \left[\frac{a_1}{q_1 + q_2} \right], \quad q_2 = \phi \left[\frac{a_2}{q_1 + q_2} \right]$$

→ Relative humidity

= $\frac{\text{Mass of water vapour} / \text{m}^3 \text{ of air}}{\text{Mass of water vapour required to saturate } 1 \text{ m}^3 \text{ of air}}$

Mass of water vapour required to saturate 1 m^3 of air

→ Rate of diffusion

Amount of gas passing through an area / unit time

→ Pressure recovery by Evance

$$= \left[\frac{v_1^2 - v_2^2}{2g} \times \eta \right] \rho g \text{ Pascal}$$

v_1 = inlet velocity at base

v_2 = outlet vel. at outlet

$$\left(\frac{1}{2} \rho v_1^2 - \frac{1}{2} \rho v_2^2 \right) \eta$$

$$\left(\frac{v_1^2 - v_2^2}{2} \eta \right) \frac{\rho}{g} \text{ mm wtg}$$

Shock Loss

→ Shock factor for bend

$$X = \frac{0.25}{t^2 \sqrt{a}} \times (i/90)^2$$

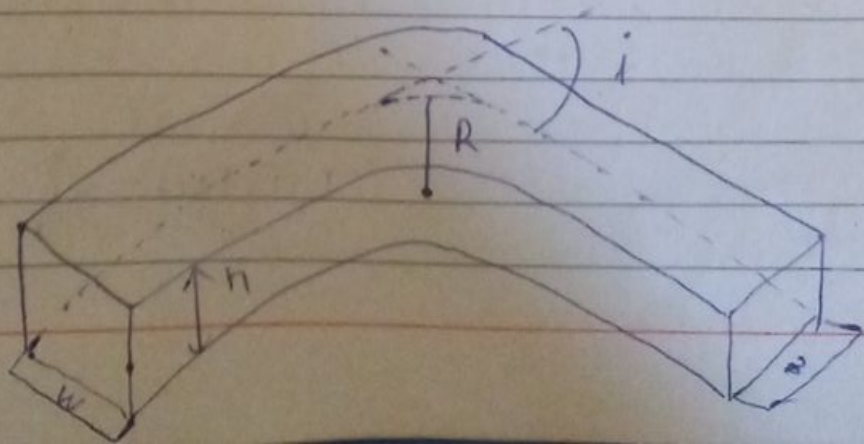
where

t = radius ratio $\left(\frac{r}{w} \right)$

a = aspect ratio $\left(\frac{h}{w} \right)$

i = deflection angle (degrees)

X = shock factor



Shock pressure loss

$$X \frac{1}{2} \rho v^2 \text{ or } X P_v \text{ (Vel. pressure)}$$

✓ ρ = density of air

✓ v = air velocity

Reynolds' number

→ Shows nature of flow of fluid
(Laminar (streamline) turbulent)

$$= \frac{VD\rho}{\mu}$$

μ = Viscosity of fluid (kg/m.s)

ρ = fl. density

D = Duct dia (cm)

V = mean vel. of flow (m/s)

Eq. dia = $\frac{4A}{P}$ → A → cr sectional area
 P → Perimeter of airway

✓ Kinematic viscosity (ν)
 $= \frac{\mu}{\rho} \text{ m}^2/\text{s}$

$$Re = \frac{VD}{\nu}$$

→ Manometric efficiency

The actual depression produced by a fan is somewhat less than the calculated theoretical depression

→ $\text{Mech } \eta = \frac{\text{Actual dep. prod.}}{\text{Theoretical dep.}}$

~~$\eta = \frac{\text{Output produced}}{\text{Input}}$~~
 → $\eta = \frac{\text{output} \rightarrow \text{air power}}{\text{Input}}$

↳ a) Power given to the fan shaft

b) Power given to the motor at engine

→ When fan shaft hp is considered as input η is called mechanical efficiency of the fan or fan efficiency

$= \frac{\text{Air hp}}{\text{Fan shaft hp}}$

→ When power given to the motor is considered as input, η is called overall mech. eff.

→ $\text{OM } \eta = \frac{\text{Air power}}{\text{Power input to fan motor + engine}}$

H = head generated by fan (m)

$(H \rho g) Q \times 10^{-3}$

$\rho = \text{air density}$

Power input to fan motor (kW)

$$\checkmark \text{ Fan motor power} = \text{Air power} \\ \eta_{\text{fan}} \times \eta_{\text{motor}}$$

Q A sealed area known to have blackdamp has 18% O_2 , 2% CO_2 , 78% N_2 . Fresh air has 21% O_2 , 0.03% CO_2 , 78.97% N_2 .

Percentage of Blackdamp in the area is?

sol

$$21\% \text{ O}_2 \rightarrow 78.97\% \text{ N}_2$$

$$1\% \text{ O}_2 \rightarrow \frac{78.97}{21}\% \text{ N}_2$$

$$18\% \text{ O}_2 \rightarrow \frac{78.97}{21} \times 18 = 67.688\% \text{ N}_2$$

$$21\% \text{ O}_2 \rightarrow 0.03\% \text{ CO}_2$$

$$1\% \text{ O}_2 \rightarrow \frac{0.03}{21}\% \text{ CO}_2$$

$$18\% = \frac{0.03}{21} \times 18\% \text{ CO}_2 \rightarrow 0.0257\% \text{ CO}_2$$

Blackdamp:

Excess N_2 + Excess CO_2

$$= (78 - 67.688) + (2 - 0.0257) \\ = 12.286\% \text{ Amv}$$

Q Find percentages of blackdamp, whitedamp, firedamp and air in a mine air sample having

$$O_2 - 19.11\%$$

$$N_2 - 79.04\%$$

$$CO_2 - 0.25\%$$

$$CO - 0.02\%$$

$$CH_4 - 1.58\%$$

What is the composition of Blackdamp?

Sol

Atmospheric air entering the mine has -

$$O_2 \rightarrow 20.93\% \quad (\text{Vol } \%)$$

$$N_2 \rightarrow 79.04\%$$

$$CO_2 \rightarrow 0.03\%$$

~~$$O_2 - 20.93\% \rightarrow N_2 - 79.04\%$$~~

$$20.93\% O_2 \rightarrow 79.04\% N_2$$

$$1\% O_2 \rightarrow \frac{79.04}{20.93}\% N_2$$

$$\rightarrow 19.11\% O_2 \rightarrow \frac{79.04}{20.93} \times 19.11$$

$$= 72.166\% N_2$$

$$20.93\% O_2 \rightarrow 0.03\% CO_2$$

$$1\% O_2 \rightarrow \frac{0.03}{20.93}\% CO_2$$

$$= \frac{0.03}{20.93} \times 19.11 = 0.0273\% CO_2$$

$$\text{Blackdamp} := \text{exc. N}_2 + \text{exc. CO}_2$$

$$= (79.04 - 72.166) + (0.25 - 0.0273)$$

$$\text{Bl (sample)} = 7.1\%$$

Atmospheric air

$$= 19.11 + 72.166 + 0.0273$$

$$= 91.3\%$$

∅ The evasee chimney of a fan has an area of 4m^2 at base and 14m^2 at outlet.

i) calculate the saving of water gauge
sol:

$$\text{Alter} \Rightarrow V_{pi} = \frac{1}{2} \rho v^2 = \frac{1}{2} \rho \left(\frac{\phi}{A}\right)^2 = \frac{1}{2} (1.2) \left(\frac{100}{4}\right)^2$$

$$\text{native} = 375 \text{ Pa}$$

$$V_{po} = 30.612 \text{ Pa}$$

$$\text{Sav. in wg} = \frac{375 - 30.612}{9.81}$$

$$= 35 \text{ mm wg}$$

⇒ ~~Gain of Pr~~

$$= \frac{V_1^2}{2g} - \frac{V_2^2}{2g}$$

$$= \frac{25^2}{2 \times 9.81} - \frac{30.612^2}{2 \times 9.81} = 7.14^2$$

$$= \frac{31.855}{1.2} = 29.256 \text{ mm} \times 1.2$$

Head of air

$$= 35 \text{ mm wg}$$

~~31.855~~

AKGoyal
Q92 sal

$$R = \frac{P}{\phi^2} = \frac{1000}{150^2} = 0.044$$

~~= 0.044 N s² m⁻⁸~~

Gain in p_i due to
evasee

$$V_{pi} A_0 = 18 \text{ m}^2$$

$$\frac{A_i}{A_0} = \frac{1}{4} = A_i = 4.5 \text{ m}^2$$

$$V_{pi} = \frac{1}{2} (1.2) \left(\frac{\phi}{A} \right)^2$$
$$= \frac{1}{2} (1.2) \left(\frac{150}{4.5} \right)^2 = 666.66 \text{ Pa}$$

$$V_{po} = \frac{1}{2} (1.2) \left(\frac{150}{18} \right)^2 = 41.66 \text{ Pa}$$

$$P_i \text{ gain} = 625 \eta$$

~~η~~ Change in p_i due
to inst. of evasee

$$= 0.044 \times 120^2$$

$$= 640 \text{ Pa}$$

$$= 1000 - 640 = 360 \text{ Pa}$$

$$\eta = \frac{360}{625} \times 100 = 57.6\%$$

Relative Humidity

= $\frac{\text{Mass of water vapour}}{\text{m}^3 \text{ of air}}$

$\frac{\text{Mass of water}}$

$\frac{\text{vapour req. to saturate}}{1 \text{ m}^3 \text{ of air.}}$

Relative Humidity

$$= \frac{\text{Act. vapour Pressure} \times 100}{\text{Saturated Vap. pressure}}$$

Humidity Ratio:

Specific humidity or Humidity ratio of an air sample is the ratio of the weight of water vapour contained in the sample compared to weight of dry air in the same sample

$$622 \left(\frac{\text{partial vapour pressure}}{\text{Baro. pressure} - \text{Saturated vap. pr.}} \right) \times 1000$$

g / m³

→ Lightest gas → H₂
SG → 0.070

Heaviest gas → SO₂
→ 2.264

Blackdamp is also called styghe or chocke damp
(mix. of CO₂ & N₂)

Firedamp → Mix. of CH₄, N₂,
Higher hydrocarbons

White damp → CO

(C₂H₆, C₂H₄),
CO₂

Stinkdamp → H₂S

Afterdamp → prod. by coal dust or
firedamp explosion

Metal trussing methodsApplications

- Room & pillar

- Development is followed by de-pillaring for max. extraction of coal pillars the standing pillars supporting the roof over the coal seams.

- Ore is extracted in wide rooms

sep by pillars of in situ ore provided in a regular manner for support of the hanging wall

→ Ore & hanging wall should be strong

→ Dip should be mild or nearly flat

→ Thick ore body

Advantage :- i) Low pt. cost

ii) Very little

disturbance of ore

iii) High level productivity

(high OMS of face workers)

Disadvantage :- i) Loss of ore in pillars

Open stopes

→ No filling at timber is used to support walls and only simple form of scattered timbering is used as temporary support.

- Both the wall racks & the ore should be strong
- Dilution of ore is minimum.

1) Overhand Stoping

- The two levels enclosing an ore block are connected to raise at intervals and stoping starts from the raise.

- Stopeation proceeds from lower main level towards the upper main level & ore is extracted in step like faces or benches in a ascending order.

- Commonly emp. in steeply dipping narrow veins and in bedded dep. of 2-3 m thickness.
- Strong ore & wall racks

ii) Roll Stoping

Geology

Minerals, rocks & their
Origin, Classification,
Ore genesis, structural
geology

Rock types

Igneous rocks

- Igneous rocks form when molten
lava or magma cools and

solidifies

Minerals:

1) Quartz ✓

Quartz, feldspar,

2) Pegmatite ✓

mica, olivine,

3) Diorite ✓

pyroxene

4) Gabbro ✓

these are the ex of intrusive igneous
rocks.

these rocks crystallize below
earth surface and

slow cooling allows

large crystals to form

Extrusive igneous rocks

→ erupt onto the surface

& cool quickly to form

small crystals

1) andesite ✓

2) basalt ✓

3) thyalite ✓

Sedimentary Rocks

→ ~~Sed~~ Sed rocks are formed by the accumulation of mineral particles or sediments at the earth surface, followed by cementation

Examples:-

- i) Sandstone ✓
- ii) Shale ✓
- iii) Siltstone ✓
- iv) Conglomerate ✓
- v) Dalarnite ✓
- vi) Coal ✓
- vii) Limestone ✓

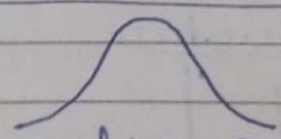
- Metamorphic Rocks
- i) Phyllite ✓
 - ii) Schist ✓
 - iii) Gneiss ✓
 - iv) Quartzite ✓
 - v) Marble ✓

→ Angle of fault

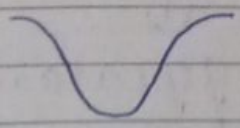
→ angle between vertical plane & fault plane

Fold

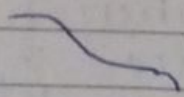
- Undulation in stratified rock masses
- anticline convex upward



- syncline concave upward



Monocline



Comminution

- Reducing the raw ore to size required for mechanical separation
- Coarse size reduction
 - ✓ Stage - Crushing
 - ✓ Fine size reduction
 - ✓ Stage - Grinding

Objectives of comminution

- i) Reduction of large lumps to small pieces
- ii) Production of solids of desired size ranges or specific surfaces for direct metallurgical treatment
- iii) Breaking apart valuable minerals from gangue material

Crusher - i) Primary crusher

ii) Secondary crusher

crusher

✓ cone crusher

✓ gyratory crusher

✓ Jaw & Gyratory crusher

✓ Blake crusher

✓ Bridge crusher

✓ Universal crusher

Cylindrical crusher:

i) Suspended spindle

type

ii) Supported spindle type

iii) Fixed spindle type.

Grinding → Breaking down

the relatively coarse

material (prod. by crushing)

to the ultimate fineness

i) Ball mill is used

$D = \text{Dia. of mill}$

$d = \text{dia. of ball}$

$g = a \cdot d \cdot u \cdot a \cdot g \cdot r$

$r = \text{rad. of ball}$

Critical Speed of mill

→ The min speed at which a

mill charge will centrifuge

is known as critical speed of mill

$$N = 54.19 / \sqrt{R} \quad \text{or} \quad \sqrt{\frac{2g}{(D-d)}} \times \frac{60}{2\pi} \text{ rpm}$$

$N = \text{Critical speed (rpm)}$

$R = \text{rad of mill (ft)}$

$$\text{or } \sqrt{\frac{g}{r}} \text{ m/s}$$

Faster the mill is rotated

higher the balls will be lifted,

when speed of rotation is

great enough, gravity is powerless

to the centrifugal force & the balls

will be carried through a

complete circle. When this happens,

the charge is said to be centrifuge.

Gate 2013

→ For spherical charge,
max allowable ratio of dia to
charge length is 1:6

~~Rift stopping method~~
Phreatic Surface

→ Also called water table

→ defined as the surface at every
point of which the pressure
in the water is atmospheric

→ Also defined as level in the
soil where the hydraulic pressure
of the water in soil pores =
atmospheric pressure

→ $P(A) = 0.5$

$P(B) = 0.4$

∴ A and B are independent

✓ $P(A \cap B) = P(A) \cdot P(B)$

✓ $P(A \cup B) = P(A) + P(B) - P(A \cap B)$

$P(A \cap B) = 0.20$

$P(A \cup B) = 0.5 + 0.4 - 0.2$
 $= 0.7$

→ Impedance = $\frac{P_{\text{wave}}}{\text{velocity of rock}} \times \rho_{\text{rock}}$

→ $\Delta m_{p_{exp}} \rightarrow \frac{V_{00} \times P_{exp}}{1000}$

→ Standard Pressure:

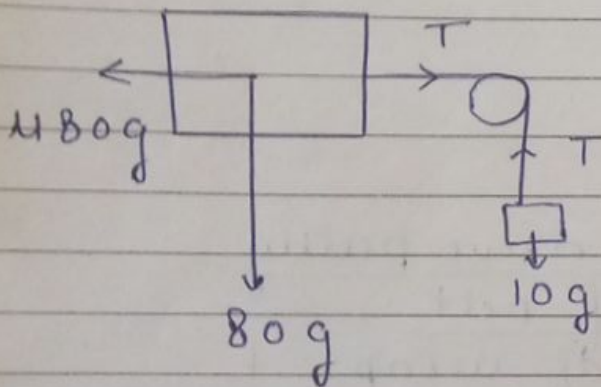
$= 101.33 \text{ kPa}$

$1 \text{ bar} = 1.013 \times 10^5 \text{ Pa}$

760 mm of Hg

$P = \rho g h$

$\frac{1.013 \times 10^5}{1000 \times 9.81} = h = 10.32 \text{ m}$



$10g - T = 10a$
 $+ T - 3.2g = 80a$
 $6.8g = 90a$
 $a = 0.74 \text{ m/s}^2$

(coal dust)

→ Explosibility factor :-

Ratio of amount of inert dust
to amount of coal dust

Am. of Limestone dust = 3g
(Inert dust)

Am. of coal dust = 2g

Exp. factor = $\frac{3}{2} = 1.5$

$$\rightarrow L_T = 20 \text{ m}$$

Actual length
= 19.8 m

$$\left(\frac{19.8}{20}\right)^3 \times 4000 = 3881 \text{ m}^3$$

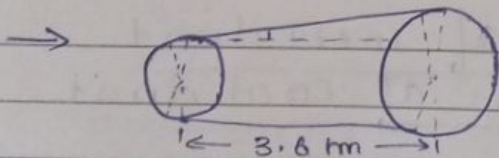
\rightarrow Respiratory Quotient /

Young's ratio =
= $\text{CO}_2 \text{ pt} / \text{O}_2 \text{ consumed}$

$$= \frac{3.83}{20.93 - 16.65} = 0.89$$

\rightarrow Snub Pulley

- \checkmark Mounted close to drive pulley
- on return side of belt
- \checkmark Increases angle of wrap around the drive pulley
- \checkmark Reduces belt tension



angle of contact of
snub pulley = $180 - 2\alpha$

$$\tan \alpha = \frac{1.2 - 0.8}{3.6}$$

$$\alpha = 6.3^\circ$$

A of contact

$$= 180 - 2(6.33)$$

$$= 167.34^\circ$$

Environmental Studies of Mine

→ Sound wave propagation

✓ Point source

$$L_p = L_w - 20 \log_{10} (r) - 11 \text{ dB}$$

↓ ↓
Sound So. power level
Pr. level of the point source

of the point source

at a radial distance

of r from the noise source

Rel. betw two sound pr. level
at a radial dist. of r_1 & r_2

$$L_{p1} - L_{p2} = 20 \log \left[\frac{r_2}{r_1} \right]$$

L_{p1} & L_{p2} → sound pr. level
at a radial distance
of r_1 and r_2 .

✓ Line source

$$L_{p1} - L_{p2} = 10 \log \left[\frac{r_2}{r_1} \right]$$

→ Illumination

→ Intensity - relative amount of
(bright, luminous energy given by
Shining) any source.

→ measured in candles or candle power or in candelas.

→ Mean spherical candle power \propto total light given by the lamp

→ Illumination of a surface (meter candle)
 $= \frac{\text{Candela of source}}{\text{dist}^2} \times \cos \theta$

θ = angle between normal to the surface & direction of light rays

→ lumen (lm) → Unit of light emitted by a light source

Lumen emitted by a lamp → Mean sph. Cand. power
 $\times 4\pi$

$$1 \text{ lux} = 1 \text{ lumen/m}^2$$

→ Footcandle (Fc) → unit of measure of illumination

$$1 \text{ Fc} = 1 \text{ lumen/ft}^2$$

$$1 \text{ Fc} = 10.764 \text{ lux}$$

→ Ultimate BOD

✓ = amount of oxygen required to decompose all the biodegradable organics in a given vol. of water.

$$BOD_t = BOD_L (1 - e^{-kt})$$

$t = \text{time (day)}$

$BOD_t = \text{BOD at any time } t, \text{ mg/l}$

$$BOD_L = \text{Ult. BOD (mg/l)}$$

$k = \text{const. representing rate of BOD reaction}$

COD > BOD
↓
chemical
ox. demand

→ In COD test, K_2CrO_7 is used to oxidize the organics

→ Total suspended solids in the filter

$$TSS = \frac{A - B}{C} \rightarrow \begin{array}{l} \text{Weight of clean filter} \\ \text{Weight of filter + retained solids} \\ \text{Volume of sample filtered} \end{array}$$

→ Equivalent Noise Level

Constant sound pr. level which would have produced the same total energy as the actual level over the given time

$$L_{\text{eq,T}} = 10 \log_{10} \left[\sum_{i=1}^m t_i 10^{L_i/10} \right]$$

eq. SPL

fraction of time for SPL L_i
time duration t_i

Day night equivalent noise level

$$L_{\text{dn}} = 10 \log_{10} \left[\frac{15}{24} (10^{L_d/10}) + \frac{9}{24} (10^{(L_n+10)/10}) \right] \text{ dB(A)}$$

L_d = day equivalent

noise level

(6 am - 9 pm)

L_n = night eq. noise

level

(9 pm - 6 am)

dB(A)

Measurement of Noise

→ Audible frequency range
of human ear
= 20-20000 Hz

Sound Pr Level - magnitude of val.
as a sound expressed in decibals

$$SPL = 20 \log_{10} \left[\frac{P}{P_{ref}} \right]$$

↓
Sound Pr. Level (dB)

$P = \text{Meas. SPL (N/m}^2)$

$P_{ref} = \text{Ref. SPL (N/m}^2)$

$(2 \times 10^{-5} \text{ N/m}^2)$

Sound Power level -

$$L_w = 10 \log_{10} \left[\frac{W}{W_{ref}} \right] \text{ dB}$$

$W = \text{acoustic power of}$
interest (watt)

Related to sound

$W_{ref} = \text{reference ac. power}$

(10^{-12} W)

Electrostatic Precipitator

→ It is a air pollution control device
that uses electric charge to remove
certain impurities, like solid particles
or liquid droplets from air or other
gases in smokestacks.

Acoustic power → Sound power at acoustic power is the rate at which sound energy is emitted, reflected or transmitted or received, per unit time.

→ TWA → Time weighted avg noise level

It shows worker's daily exposure to occupational noise, taking into account the avg. levels of noise & time spent in each area

Noise Dose

$$= 100 \times \left(\frac{c_1}{T_1} + \frac{c_2}{T_2} + \dots + \frac{c_n}{T_n} \right)$$

C = Time sp. at each noise level.

$$T_n = \frac{8}{2} \times \frac{\text{Power}}{(L-90)/5}$$

L = Mean sound level

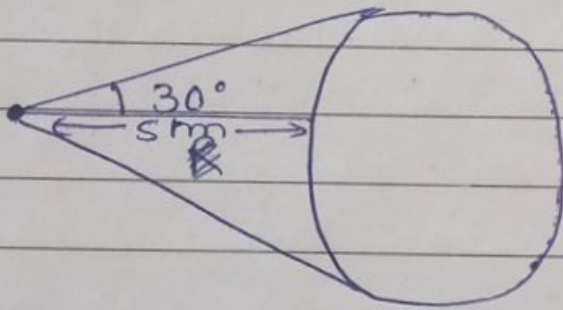
$$T_1 = \frac{8}{2} \left(\frac{4}{5} \right) = 13.93$$

$$T_2 = \frac{8}{2} (0.4) = 6.06$$

$$\text{Dose} = 100 \times \left(\frac{6}{13.93} + \frac{3}{6.06} \right) = 92.57\%$$

$$\checkmark \checkmark TWA = 16.61 \log [D/100] + 90$$

$$16.61 \log 0.9257 + 90 \\ = 89.4 \text{ dB}$$



For plane angle

Surface area covered by
beam = πR^2

For solid angle

$$SA = \frac{2\pi}{2\pi} (1 - \cos \theta) R^2$$

$2\pi(1 - \cos \theta) \rightarrow$ Solid angle (rad.)

Drilling

→ Top hammer drilling

→ Used in medium to hard rocks
for hole dia. up to ~~230mm~~
top hammer drills include

- i) Hand held rock drills
(Stoppers, Jack legs, sinkers)
- ii) light drills mounted on a
feed device and boom for
tunneling (jumbos)
- iii) medium to heavy crawler
based or wheel based
drill rigs. ~~with boom~~

THD combines → Percussion-
feed-rotation-
flushing

→ In THD, hammer produces
a percussive force on drill rods
which is transmitted to the
drill bit

Benefits

- i) Faster penetration rate as
comp. to DTH
- ii) Highly mobile
- iii) Lower fuel consumption

Detonator

- Used to trigger explosive device
- commercial use of explosives uses electrical detonators at the capped fuse which is a length of safety fuse to which an ordinary detonator has been crimped.

Explosives

ANFO (Ammonium Nitrate Fuel Oil)

- i) Ammonium nitrate mixed with diesel oil, is (94%)
(6%) used on a large scale for blasting in quarries of coal and metal mines.

NOV → 3.2 km/s Form = All solid

Size → 2 mm

ii) Slurry explosives

gelling agents - starch

Fuel → TNT, PETN
Sensitizers

Slurry explosives are with jelly like consistency & are water gels

Ingredients - Oxidizers → ammonium, sodium or calcium nitrates
Cross linking agents → potassium or sodium dichromates

→ Slurry & Emulsion exp. are highly water resistant.

→ Size → 0.2mm

Form → Solid Liquid

VOD → 3.3 km/s

Emulsion explosives

→ Contains AN solution comb. with diesel oil

→ depend entirely on presence of voids for initiation & propagation

effects a change in density
→ More fluid than slurry exp. & therefore create

problems when a loading a blast hole with fissures or cracks

→ Size → 0.001mm

Form → Liquid

VOD → 5-6 km/s

Advantages of Nobel System

i) Extreme resistance to accidental initiation

ii) Noiseless in character

iii) eliminates the need for

complicated electrical circuit testing & shot firing equipment

- (iv) eliminates the risk of misfire
- v) Full exploitation of explosive energy & minimizes flyrock
- vi) Reduced vibration & better rock fragmentation is achieved

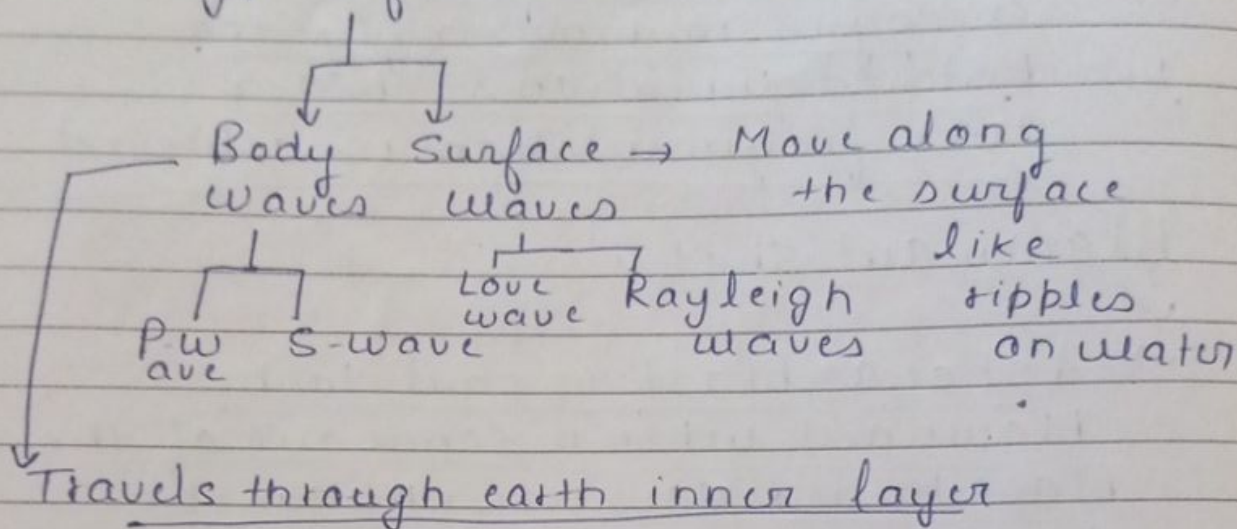
Blow out shot

- A shot or blast is said to be blow out when it comes out of the blast hole & does not shatter the rock
- Such shots dissipate the explosive force by blowing out of the stemming instead of breaking down the coal
- Occurs due to improper stemming, excessive burden or spacing blow shot holes, improper use of delay detonators incorrect sequence of firing of shot holes.
- Seismic Waves

Waves of energy caused by sudden breaking of rock within the earth or an explosion

Recorded on Seismographs

Types of seismic waves



Body waves travelling through the interior of the earth, body waves arrive before the surface waves emitted by an earthquake

- P wave → also called primary, compressional and longitudinal waves
- In solid, travels fast as twice as S waves
 - Fastest seismic wave
 - can travel through any type of material.
 - Pushes & pulls the rock it moves

- S-wave → also called secondary, transverse or shear waves
- Slower than P wave
 - Move through solid but not liquid medium

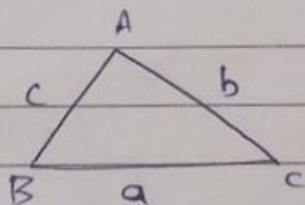
→ ground is displaced perpend. to
the direction of propagation.

Love waves → Fastest Surface waves
→ causes horizontal
shearing of ground
→ travel faster than
Rayleigh waves

Rayleigh waves → also called ground
roll
→ travels as ripples
with motions similar
to waves on water surface

Trilateration

Trilateration, method of surveying in which the lengths of the sides of a triangle are measured and from this inf., angles are computed



Cosine rule

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$b^2 = a^2 + c^2 - 2ac \cos B$$

$$c^2 = a^2 + b^2 - 2ab \cos C$$

$$\text{Sin Rule} = \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Triangulation

→ It is the process of measuring the angles of a chain or network of triangles formed by stations.

Mine Machinery

→ Centre to centre distance
✓ blw two spur gears

$$PD_{G_1} + PD_{G_2}$$

$$\frac{(N_1 + N_2) m}{2}$$

$$PD_{G_1} +$$

$PD_{G_2} =$ Pitch Dia of Gear 1 & 2

$m =$ module of gear

$N_1 \& N_2 =$ No. of teeth in Gear 1 & 2.

→ Centrifugal Ratio

$$= \frac{\text{Cent. force}}{\text{Weight of vehicle}}$$

$$= \frac{m v^2 / R}{m g} = \frac{v^2}{g R}$$

→ Input power (w)

$$= \sqrt{3} \times PF \times V I$$

PF = Power factor
= $\cos \phi$

V & I = Voltage
current

$$P = \frac{F \times v}{F \times \frac{D}{t}}$$

= Work done per unit time

Mine Pumps

Mine pumps works on Bernoulli's theorem which states

When a fluid flows through a passage of varying cross section, total energy of moving stream remains constant, assuming no friction losses.

Pumps laws

or D (Imp. dia) (BHP)

i) $Q \propto N$ (rpm)

$P \propto N^3$ or D^3

Quantity of water

$P \propto N^2$ (rpm) or D^2

Power required

Pressure / Head

developed by each impeller

$\rightarrow \eta$ (Efficiency) = $\frac{\text{Power Output}}{\text{Power Input}}$ ✓

\rightarrow Mechanical

efficiency of pump

HP in water

HP input to ✓

pump shaft

\rightarrow Darcy formula for

head loss due to friction

$$= H_f = \frac{4fLV^2}{2gd}$$

V = vel. of flow (m/s)

f = coeff of friction

L = pipe length (m)

d = pipe dia (mm)

Manometric efficiency

= $\frac{\text{Mano. Head (H)}}{\text{Work head imparted by the rotor on the fluid / Euler head}}$

$$= \frac{H}{(vU/g)}$$

U = tangential velocity of the imp. at outlet $(\frac{\pi DN}{60})$
v = whirl velocity at outlet

~~v~~ ~~U~~ ~~v~~

$$\text{Man. eff.} = \frac{\text{Actual Head}}{\text{Theoretical head}}$$

Locomotive

→ Limiting gradient against the load for the loco transportation is 1 in 15 but generally adapted on gradients milder than these gradients.

Diesel Locomotives

- Locomotives used in ulq coal mines have the power unit in a flame proof enclosure as a

Safeguard against ignition of firedamp.

- Max. permissible CO in exhaust gases is 0.2%.
- Max. permissible angle for conveying coal in PVC belt conveyor is 16°.

Gear Calculation

Diametral pitch → describes gear tooth size

$$P = \frac{N}{D}$$

↓ No. of teeth
pitch dia.

Pitch dia → Dia. of pitch circle
 $D = \frac{N}{P}$ → No. of teeth
P → diametral pitch

Gear Ratio = $\frac{\text{No. of teeth on driven gear}}{\text{No. of teeth on drive gear}}$

Velocity of gear

$$= \frac{\pi DN}{60} \text{ (m/s)}$$

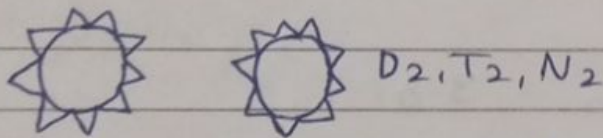
→ Circular pitch = Circumference of pitch circle
No. of teeth

No. of teeth = Circumference of pitch circle
Circular pitch

Circular pitch → dist. between two consecutive teeth, centre to centre, as measured along the pitch circle

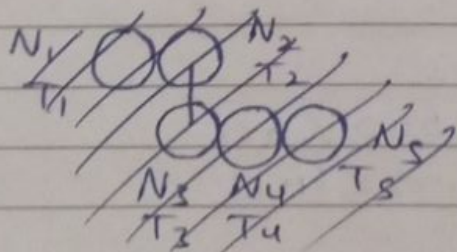
Module → $\frac{D \text{ (Pitch Dia)}}{N \rightarrow \text{No. of teeth}}$

Gear trains



D_1, T_1, N_1 → speed (rpm)
 ↓ ↘ No. of teeth
 Pitch dia

$$\frac{N_1}{N_2} = \frac{D_2}{D_1} = \frac{T_2}{T_1}$$



$$\frac{N_1}{N_5} = \frac{N_2}{N_4} \times \frac{N_4}{N_3} \times \frac{N_3}{N_5}$$

$$= \frac{T_2}{T_1} \times \frac{T_4}{T_3} \times \frac{T_5}{T_4}$$

Vel.

Ratio

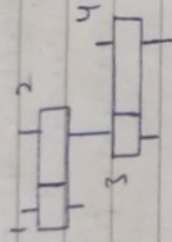
= $\frac{\text{Sp. of follower wheel}}{\text{Sp. of driver wheel}}$

$$\frac{N_1}{N_5} = \frac{T_2}{T_1} \times \frac{T_4}{T_3} \times \frac{T_5}{T_4}$$

$$\frac{N_2}{N_1} = \frac{T_1}{T_2} \quad \frac{N_3}{N_1} = \frac{N_2}{N_1} \times \frac{N_1}{N_3}$$

$$\frac{N_3}{N_2} = \frac{T_2}{T_3} = \frac{T_1}{T_2} \times \frac{T_2}{T_3} = \frac{T_1}{T_3}$$

Comp train



$$\frac{N_2}{N_1} = \frac{T_1}{T_2}$$

$$\frac{N_4}{N_3} = \frac{T_3}{T_4}$$

$$\frac{N_2}{N_1} \times \frac{N_4}{N_3} = \frac{T_1}{T_2} \times \frac{T_3}{T_4}$$

$$N_2 = N_3$$

$$\frac{N_4}{N_1} = \frac{T_1}{T_2} \times \frac{T_3}{T_4}$$

AK Gorai Imp. Questions

Q3 sol

$$G_{\text{first gear}} = 3.81:1$$

$$TC \rightarrow 2.72:1$$

$$D_{\text{diff}} \rightarrow 4.11:1$$

$$V = \frac{\pi D N}{60}$$

$$= \frac{3.14 \times 1.2 \times 1000}{60}$$

$$= 3.81 \times 2.72 \times 4.11$$

$$V = 5.3 \text{ km/h}$$

Ans

$$\rightarrow \text{rms torque} = \sqrt{\sum_{i=1}^n \tau_i^2 t_i} \rightarrow \text{Torque (Nmm)}$$

$$V \sum_{i=1}^n t_i \rightarrow \text{Time period}$$

Head is the measurement of
pr. req. to successfully
deliver the fluid pumped
at the desired flow

$$H = \frac{V^2}{2g} \text{ (ft)}$$
$$\rightarrow 32.2 \text{ ft/s}^2$$

→ Total Suction Head

Read. of gauge on the suction

ii) Watery places & corrosive atmos Locos

- Limiting gradient for loco transportation is 1 in 15 but generally adopted for milder than 1 in 25.

✓ Diesel locomotives

- Locos used in ulg mine have the power unit in a flame proof enclosure as a safeguard against ignition of firedamp.
- Max. permissible CO in exhaust gases is 0.2%.

✓ Electric Battery locomotive

- Less powerful than diesel and tralley wire locomotive
- Quiet in operation and produces no objectionable fumes & generates much less heat as comp. to diesel loco.

Mining Methods

- Max. possible faces = $3m-2$
- Min. faces available = m
- avg. no. of faces avail. = $\frac{2m-1}{h}$
- no. of headings

Conditions for Longwall Mining

- Depth → Moderate to very deep
- Dip → (Flat & uniform) (Dip should be less than 12°)
- Deposit → Tabular / Shape

Roof strength → It should be crush under roof pressure rather than yield, preferably material that is weak and can be cut by continuous miner.

Rock strength → Weak to moderate, must break and cave.

Overhead wire locomotive

- DC current is supplied through the overhead wire to supply power
- Max. efficiency, high overload capacity, simple maintenance
- A good reliability as compared to others.

Mining Methods - Applications

Ram & Pillar

- i) Ore with horizontal or flat dip
 - ii) Stable ore & hanging wall
 - iii) ~~is ore body up to 12m thick~~
Thick ore body
- Long Hole / Blast Hole Stoping

i) Steeply dipping ($> 50^\circ$) or vertical ore body

~~iii)~~ Shrinkage Stoping

- i) Ore body of steep dip
- ii) thickness of ore body (Thick ore body)
between 3-12m
- iii) Ore must not decompose; Oxidize as close in storage for longer duration in stope
- iv) Regular ore boundaries
- v) Stable hanging wall and footwall
- vi) Ore should be of free flow characteristics

Sublevel Stoping

- i) Steeply dipping ore
- ii) Thick ore body (4-60m)
- iii) Stable Hang wall and Footwall
- iv) Competent ore body
- v) Regular ore boundaries

Breast Stopping

- i) Preferred for low grade ore deposits
- ii) ore & wall rocks should be strong
- iii) Suitable for horizontal or mild dip & upto ~~cm~~ thick lying at moderate depth & cut & fill stoping
 thick here.
- iv) Steeply dipping but can be applied to mildly dipping also
- v) Wall rock can be loose, loosed and almost any type.
- vi) It is suitable where ground surface should be protected from subsidence
- vii) High grade ore to compensate extra cost of filling
- viii) Ore should be weakened but should sustain the rock balancing during stoping.

Sublevel caving

- i) Alb and ore should be of weak nature
- ii) Steeply dipping
- iii) Massive ore body

Sublevel top slicing

- i) Thick deposits of horizontal extent
(Suit. thickness - 6-8m)
- ii) Weak walls & alb
- iii) Ground surface allowed to subside
- iv) Salt ore, which is weak enough to stand without support only for a short period

Block caving

- i) Steeply dipping & massive ore bodies
- ii) Fairly regular ore bodies
- iii) Surface is allowed to cave
- iv) Low grade ore
- v) Weak ore to cave under its own weight

Reversing

i) Steep vein

ii) vein is valuable enough to pay for the unprofitable work of blasting down a sizeable quantity of barren wall

Square set stapling

↳ where the walls of the are body
and back of the staples are
wreak & do not stand without

subpart

↳ High grade are

Block caving

- In block caving the ore is divided in large blocks & at the bottom the block is completely undercut i.e. a horizontal slot is blasted, which removes the support of the overlying ore.
- The undercutting creates a series of fractures in the ore body which gradually affects the whole body block.
- The ore at the lower part of the block is crushed by cracked upper portion & gives a fragmentation which allows the ore to be drawn through a network of finger raises & draw point.
- Dr. & Blasting is required only in lower portion of ore body. The upper portion caves down.

Post pillar method

- It is a variant of cut & fill deposit
- Applies to inclined deposits
- Narrow pillars are left in the ore at regular intervals, to give additional strength to prevent hanging wall to footwall closure after staking.

→ While filling material surrounding the narrow pillars provides them with lateral support & prevents them failing through buckling under load operations.

Unbiased estimator

→ An unbiased estimator is an accurate statistic that's used to approximate a population parameter.

→ If the estimator (i.e. the sample mean) equals the parameter (i.e. the pop. mean) then it's an unbiased estimator.

$$E(\mu) = E(\bar{x})$$

$$E(\mu - \bar{x}) = 0$$

~~Sub level casing~~

→ The body is divided into

Sub level top slicing

→ This method is classified as a caving method as the ore caves in in top slicing the stopping unit is termed as slice

→ Ore is mined out in a series of horizontal slices by drilling & blasting beginning at the top of the ore body. Immediately beneath ore as the ore falls first slice is being taken out timber supports are erected on the floor of slice.

Greaser

Mine cars

Granby cars

- Provided with side discharge doors
hinged at the top ~~and~~
- Can handle heavier cars
- One side dumping
- Few for small gauge
curvatures
- Greater capacity
- One of these side doors are fitted
with a roller at mid height and when
the car passes by the side of a sloping

dam, the water passes over the
latter, this resulting in gradual
opening of the slide doors
and the contents are discharged.

~~Gate~~ Minepumps

~~Gate~~ 2017

Mine Survey

Avg. photo scale

→ Correction for curvature of earth

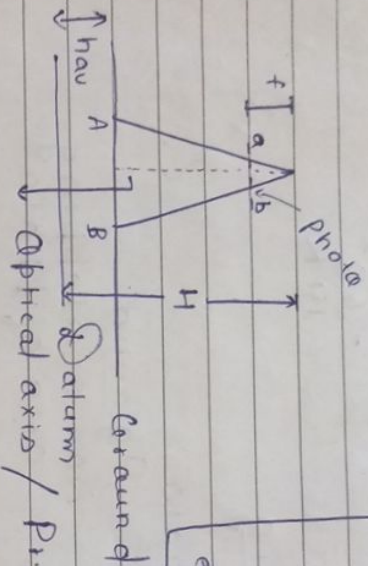
→ Correction is subtractive

Scale → Photo dist. / Ground dist.

$$\left(\frac{D}{d}\right)^2 = 0.0785 \frac{D^2}{d^2}$$

dist. b/w 1.5 & 5.5.

True staff Reading = Observed staff reading - $0.0785 D^2$



Scale of photogram / Avg. photo scale = $\frac{f}{H - h_{av}} = \frac{ab}{AB}$

Scale depends upon ground

elevation & it increase with elevation
A line on the ground have diff. elevations

Avg. elevation = $\frac{h_1 + h_2 + \dots + h_n}{n}$

$h_1, h_2, h_3, \dots, h_n$ → ground height at n no. of points

→ Correction for Refraction :- Correction is additive = $0.0112 D^2$ ($\frac{D^2}{7d}$)

True Staff Reading = Observed Staff Reading + $0.0112 D^2$

Combined Correction

- Correction of Refraction of
+ correction of
refraction

$$= \frac{-60^2}{14R}$$

$$\frac{1}{2} \times \frac{1}{3} \times \frac{0.4}{2}$$

Overlapping

→ No. of photos

= Ground

Non overlapping
area of photo

Ex:

Scale of
photograph

$$= 5000 \rightarrow 1 \text{ cm}$$

Size photograph = 18 cm x 18 cm

$$O_L = 60\%$$

$$A = 110 \text{ km}^2$$

$$O_S = 30\%$$

No. of photograph

$$= 110$$

$$(1-0.6) \times \frac{50 \times 18}{1000} \times (1-0.3) \times \frac{50 \times 18}{1000}$$

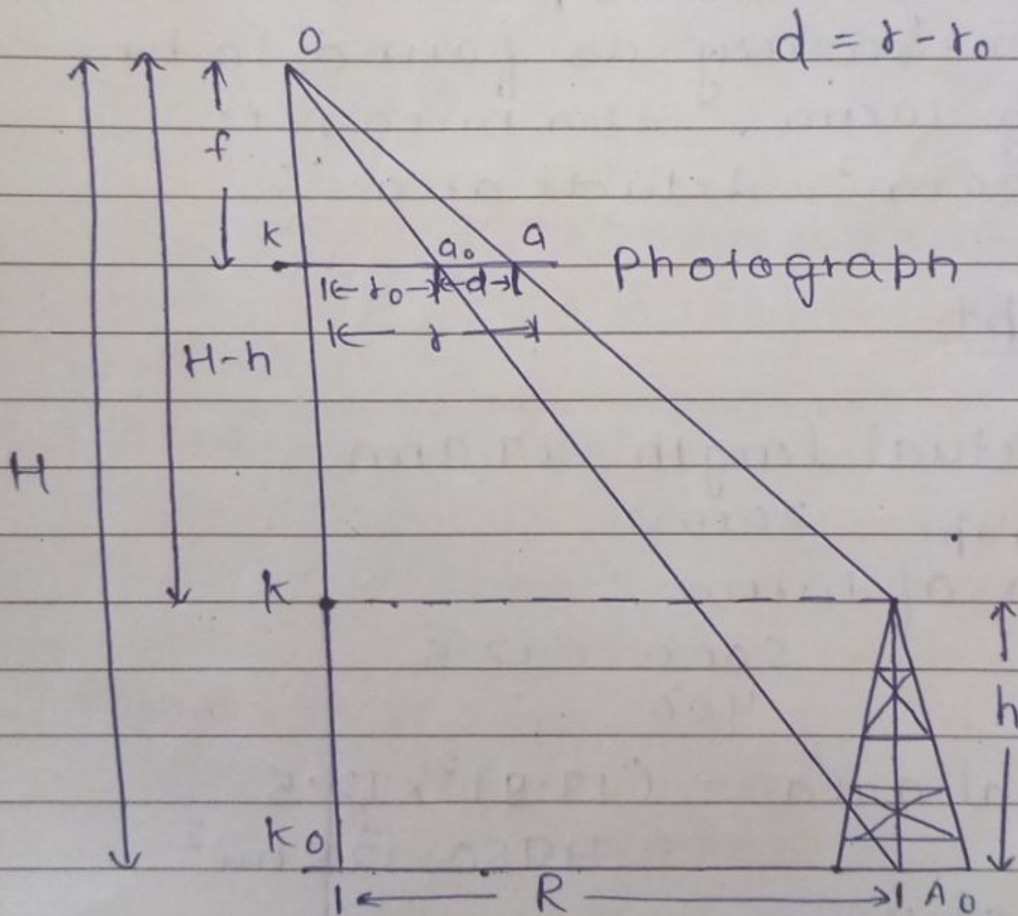
$$= 485$$

→ ~~$K \neq$ length of photo $(1-10)$~~
Scale

~~use~~

Relief Displacement

→ Shift in an object image position caused by its elevation above a particular datum.

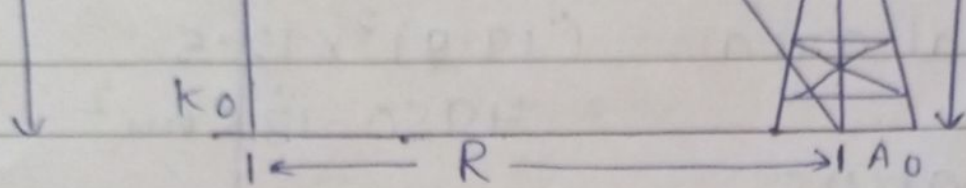


$$360^\circ \rightarrow 24 \text{ h}$$

$$1^\circ \rightarrow 4$$

$$1' = \frac{1}{15}$$

$$1'' = \frac{1}{15''}$$



$$1'' = \frac{1}{15}''$$

Q Convert $5^\circ 15' 25''$ to hrs, min & Sec

Sol

$$360^\circ \rightarrow 24 \text{ hrs}$$

$$(360 \times 60 \times 60)'' \rightarrow (24 \times 60 \times 60) \text{ Dec}$$

$$18925''$$

$$= x''$$

$$x = 24 \times 60$$

$$\times 60 \times$$

$$18925$$

$$360 \times$$

$$60 \times 60$$

$$5^\circ 15' 25''$$

$$(5 \times 60 \times 60)'' + (15 \times 60)'' + (25)''$$

$$= 18925''$$

$$(360^\circ \times 60 \times 60)'' = (24 \times 60 \times 60)''$$

$$x = 1261.66 \text{ Dec}$$

$$x = \frac{1261.66}{60} = 21.027 \text{ min.}$$

$$= 0.0277 \times 60$$

$$= 1.66 \Delta$$

$$\rightarrow 21 \text{ min } 1.66 \Delta$$

Q A 20m long steel tape used for survey is found short by 10cm. Area meas

Rock Mechanics

→ Radial stress on the excavation boundary of circular tunnel is always zero.

→ Texture → Grain size distribution of rock.

→ An longitudinal caving, the thickness of immediate roof is calculated from

$$d \leq d_0$$

d_0 = max. allowable sagging

$H - d$ = $\begin{matrix} \text{mining} \\ \text{height} \end{matrix}$

→ Sagging

of lowest uncaused

strata

$$h_{im} = \frac{H-d}{k-1}$$

✓ if $d = d_0 = H$, then $h_{im} = 0$

if $d = d_0 = 0$

$$h_{im} = \frac{H}{k-1}$$

→ Seam thickness Δ
Bulking factor

→ Horizontal mining

✓ Bulking factor - Val. of a quantity of moist granular material

Val. of same quantity when dry

→ ✓ Bulk modulus → Hydrostatic pressure
Volume strain

✓ ϕ system → Rock mass quality

$$\phi = \frac{RQD}{J_n} \times \frac{J_t}{J_a} \times \frac{J_w}{SRF} \quad RQD \rightarrow \text{Size of joint rock}$$

J_n = Joint set number

(Size of intact rock blocks in the rock mass)

✓ J_a = Joint alteration number
(shear strength along the discontinuity planes)

✓ SRF = Stress reduction factor
(Stress env. on the intact rock blocks)

✓ J_t = Joint toughness number

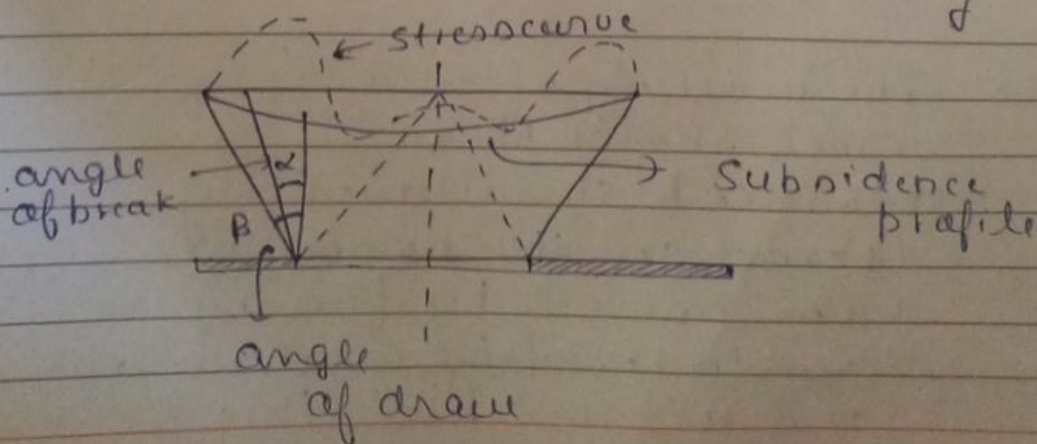
✓ RQD = Rock quality designation

✓ J_w = Joint water parameter

→ ✓ $RMR = 9 \log(\phi) + 44$

ϕ → Rock mass quality

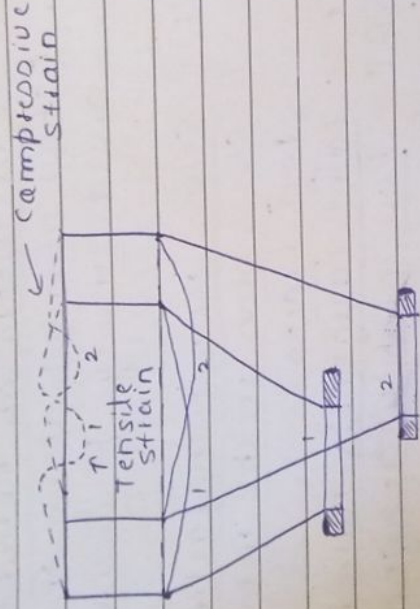
RMR → Rock mass rating



Angle of break in subsidence

→ the vertical line at the panel edge & line connecting the panel edge and the point of max. tensile strain on the surface

Harmonic method of extraction



→ Extraction of a panel causes tensile and compressive strain at the surface

→ The working of two beams should be so advanced simultaneously to cancel out the balance of strain caused by face by the strain induced by another beam at a different level this is called harmonic mining.

- By using this method, subsidence is minimized or avoided
the width of extraction is decided on basis of depth & geological factors. hence a single seam can have different extraction widths at different elevations
- bottom working has less width of extraction and topmost working has comparatively more width.

→ Dilatancy → Increase in volume due to cracking of rock

→ Birniawski's RMR considers the following parameters

- i) RQD
- ii) Spacing of Joints
- iii) Condition of Joints
- iv) Ground water condition
- v) Uniaxial comp. strength

→ Rack bumps → Violent burst of coal pillars due to sudden release of elastic strain energy stored in the pillars

→ Flat Jack → Meas. of stress acting

Barchalo deformation

gauge → Meas. of in situ rock stresses using overcoring technique

Tape extensometer → Roof
convergence

Baschale extensometer →
used for
measurement
of deformation
of rock mass

Baschale penetrometer -
Bed separation
resistance

→ The load at which an axially loaded prop reaches its elastic limit or at which it begins to buckle is called 'load bearing capacity'

→ The load on a prop when upper member begins to slide is 'yield load'

→ Freshly exposed roof after blasting is effectively & quickly supported by 'Safari Supports'

→ Residual stress is the stress due to weight of strata.

→ Roof is easily cavable
at the pratyakon index is
7 to 8

✓ The fall which takes place
soon after withdrawal of
supports is called 'local fall'

→ ✓ Volumetric Strain

$$E_v \text{ at } \Delta V = E(1-2\nu)$$

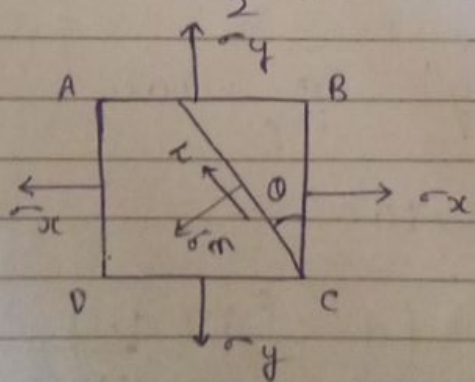
$$\nu = \frac{(\sigma_1 + \sigma_2 + \sigma_3)(1-2\nu)}{E}$$

ν = poisson's ratio
 $\sigma_1, \sigma_2, \sigma_3$ = principal stresses

→ ✓ If principal stresses are
given

$$\sigma_n = \left[\frac{\sigma_x + \sigma_y}{2} \right] + \left[\frac{\sigma_x - \sigma_y}{2} \right] \cos 2\theta$$

$$\tau = \frac{\sigma_x - \sigma_y}{2} \sin 2\theta$$



Angle of max. shear = $45^\circ + \phi$

Angle of principle plane = $\tan^{-1} \frac{2\tau_{xy}}{\sigma_x - \sigma_y}$

$$= \frac{2\tau_{xy}}{\sigma_x - \sigma_y}$$

$$\phi = \frac{1}{2} \tan^{-1} \frac{2\tau_{xy}}{\sigma_x - \sigma_y}$$

→ ✓ If σ_i → insitu stress
 σ_c → induced stress
Stress conc. at → $\frac{\sigma_c}{\sigma_i}$
that point

→ Permeability

$$\phi = KIA$$

ϕ = Flow through area
 A (m^3/day)

I = hyd. gradient ($\frac{dh}{dL}$)

k = Coeff. of permeability
or hyd. conductivity
(m/day)

A = cross-sectional area (m^2)

$$V = \frac{k}{\eta} i$$

η → Porosity

$$Sp \cdot qz = \frac{W}{W-S}$$

W = Weight in air

S = Weight in water

→ Elastic strain energy (U) = $\frac{P^2 L}{2AE}$

$$V_p = \sqrt{\frac{4/3 \sigma + k}{\rho}}$$

ρ = rock density

σ = Shear modulus

k = Bulk modulus

$$V_s = \sqrt{\frac{\sigma}{\rho}}$$

→ Resilience/unit Volume (Strain energy absorbed/unit Volume)

$$U = \frac{\sigma^2}{2E} \quad \& \quad R = U = \frac{\sigma^2}{2E} \times \text{Vol}$$

→ Vol. strain = $\frac{\Delta V}{V} = \epsilon(1-2\nu)$

$$\frac{(\sigma_1 + \sigma_2 + \sigma_3)(1-2\nu)}{E}$$

$\sigma_1, \sigma_2, \sigma_3 = \text{pr. stresses}$

→ Mohr-Coulomb failure criterion

Uniaxial comp. strength (σ_c)

$$= \frac{2c \cos \phi}{1 - \sin \phi}$$

$$\text{UTS}(\sigma_t) = \frac{2c \cos \phi}{1 + \sin \phi}$$

$c = \text{Cohesive strength}$

$$\frac{\sigma_c}{\sigma_t} = \frac{1 + \sin \phi}{1 - \sin \phi}$$

$\phi = \text{friction angle}$

Punch Shear test

↑ Shear strength

$$S = \frac{P}{\pi d t} \quad (\text{kg/cm}^2)$$

$P = \text{load applied (kg)}$

$t = \text{thickness of disc (cm)}$

$d = \text{dia of Puncher (cm)}$

Saturated Density

$$\rightarrow \frac{G + e}{1 + e} P_w$$

$$\left(\frac{W_s}{V} \right)$$

$$\gamma_d = \frac{G \cdot \gamma_{wul}}{1 + e}$$

Dry Density ($\frac{M_s}{V}$)

$$\rightarrow \frac{G \gamma_{wul}}{1 + e} = (1 - m) \gamma_{wul}$$

→ Placer Mining

→ Sluicing is used in placer mining, is the process of using a sluice box to separate gold from gravel and ore found in placer deposits situated in streams & rivers

→ Sluicing typically follows panning. Panning is used to gather a sample from a placer deposit and sluicing is used to process larger amounts of gravel for maximum gold recovery.

→ Sluicing in its simplest form is accomplished by shovelling material and gravel directly from the bottom of the river or stream into the sluice box which is placed where water is directed & gold gets trapped in riffles affixed to the bottom of the box.

→ Apart from coal, longwall mining method is also used for pyrite & phosphate mining

Common method of exploration drilling

i) Percussive with rods

Type of Bit Used → chisel shaped
Rock Formation → Sedimentary
for application → rocks of soft
or medium

→ Used for
lower drill depth or fissured
formations

ii) Churn drilling or cable drilling

→ Steel choppy bits
are used.

→ In placer deposits

Rotary Drilling

i) Non coring → Tricone rock roller bits
are used

→ Any rock formation
except very hard

ii) Diamond
drilling → Diam. bits of
various types
tungsten carbide
bits

→ Used for larger depth

→ Any rock formation
except fissured

iii) Calyx or
unsuitable → chilled
in soft & shot
fissured drilling
formation

→ Used for larger
diameters

→ Calyx bit is used
→ All rocks except the
hardest

→ $Nx > Bx > Ax > Ex$
NW

→ Base charge of detonators → PETN
Priming charge → ASA

→ Cast blasting

→ Casting of oil by explosive on cast
blasting is defined as use of
blasting to move oil directly
to the oil pit without
rehandling. It is used for
controlled flow of oil.

Mine Economics

Payback period

→ It ignores time value of money
→ It is length of time required
✓ to recover the cost of an investment

→ Project is only chosen when
✓ NPV is +ve

→ For acceptance of investment
✓ project

Payback period < cut off period

↓
pre-determined
length of time for
an investment to
be recovered

CPM - Activity Oriented technique
PERT - Event Oriented technique

Profitability Index

$$\text{If } PI > 1 = \sum_{t=1}^n \frac{CF}{CI(t)}$$

accept the project
if $PI < 1$

Reject the project

- Positive slack - indicates ahead of schedule
- Negative slack - behind schedule
- Zero slack - on schedule

→ In perpetual inventory system is intended as an material is checked when it reaches its minimum value.

Depletion Method

Capacity → 200000 T
 Cost → 200000 ₹
 extraction

Year → 1 8000 T
 2 7000 T
 3 5000 T

For 1st year
$$\frac{200000 \times 8000}{200000} = 80000 \text{ ₹}$$

For 2nd year
$$\frac{200000 \times 7000}{200000} = 70,000 \text{ ₹}$$

For 3rd year
$$\frac{200000 \times 5000}{200000} = 50,000 \text{ ₹}$$

30) Depletion allowance for 1st year

$$= \frac{75000}{500000} \times 2000000$$

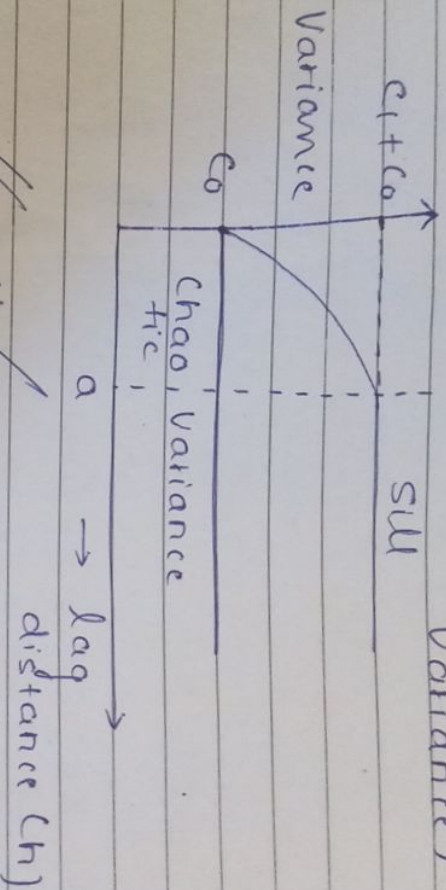
$$= \text{₹ } 300,000$$

Applicable for waste assets.

Geostatistics

→ Sill Value → $c_0 + c_1$

(Chaotic Variance + Structured Variance)



→ Scattergram

$$\hat{R}(h) = \frac{C_0 + \text{Covariance}}{\text{Sill Value}}$$

→ Semi Variance

$$= \text{Sill Value} -$$

Covariance

$$r(h) = \text{Sill} - c_0$$

→ ~~$$\varphi = \mu + z \frac{\sigma}{\sqrt{n}} \rightarrow \text{st. deviation}$$~~

$$z = \frac{x - \mu}{\sigma}$$

St. normal variate

→ Coeff. of correlation = R

Coeff. of determination = R²

↓
Explained variation of the regression model

blw two variables

→ ~~Sample covariance~~

$$= \sum_{i=1}^n \frac{(X_i - \bar{X})(Y_i - \bar{Y})}{n}$$

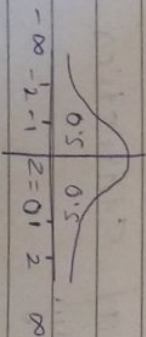
~~Standard normal variable~~

Normal dist. $f(x) = \frac{1}{\sigma \sqrt{2\pi}} e^{-1/2 \left[\frac{x - \mu}{\sigma} \right]^2}$

↓
th standard normal variable

$$Z = \frac{X - \mu}{\sigma} \quad \mu = 0 \quad \sigma = 1$$

$$f(z) = \frac{1}{\sqrt{2\pi}} e^{-z^2/2} \quad -\infty < z < \infty$$



Confidence interval

→ The confidence interval

constructed from sample data is the range of values that is likely to include the population parameter

at same specified confidence level

→ Conf. interval for a popul. mean is determined by taking the sample mean, the point estimate and subtracting & adding margin of error to it.

$$\bar{X} \pm E$$

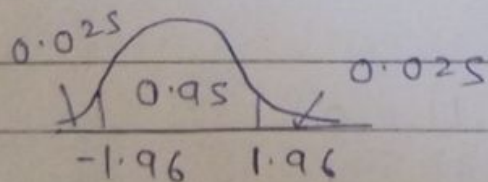
If σ is known \rightarrow Critical value
 $E = Z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$

α = Significance level
(1 - confid. level)

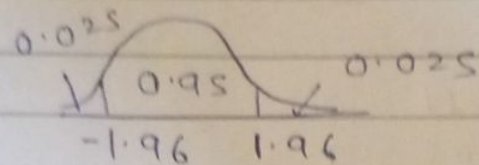
$$CL = 1 - \alpha$$

$$CL = 0.95\%$$

$$\alpha = 1 - 0.95 = \frac{0.05}{2} = 0.025$$



$$Z_{\alpha/2} = Z_{0.025} = 1.96$$



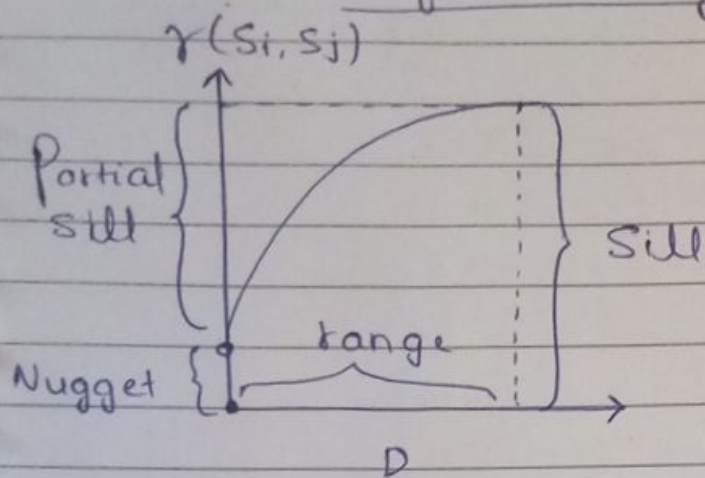
$$Z_{\alpha/2} = Z_{0.025} = 1.96$$

→ Applications of Statistics
in a/c body

Semivariogram →

Semivariogram depicts
the spatial autocorrelation
of the measured sample points

→ Once each pair of locations is plotted, a model is fit through them.



→ If two locations, s_i & s_j are close to each other in terms of distance meas. of $d(s_i, s_j)$ they are likely to be similar, so the diff. in their values, $z(s_i) - z(s_j)$, will be small

→ If s_i & s_j are far apart, they become less similar $z(s_i) - z(s_j)$ will become larger

→ Var. of diff increases with distance

$$\gamma(s_i, s_j) = \frac{1}{2} \text{var} [z(s_i) - z(s_j)]$$

Sill → Height of Semivariogram reaches when it levels off
 ↓
nugget effect + Partial sill

Range \rightarrow dist. at which the
semivariogram levels off
to the sill is called range.

Mensuration

Square = Area = a^2
P = $4a$
A = a^2

Rectangle = Area = lb
P = $2(l+b)$
A = lb
D = $\sqrt{l^2+b^2}$

Parallelogram = $b \times h$

Trapezium = $\frac{h}{2}(a+b)$

Circle = Area = πr^2
P = $2\pi r$
Area = $\frac{\pi d^2}{4}$

Semi circle = $\frac{\pi r^2}{2}$
P = $\pi r + 2r$

Right angle triangle = $\frac{1}{2} \times b \times h$

~~80 Ps = Ps + 60 + 60 - 40 Pa~~

(1-2) 10

Cube

$$V = a^3$$

$$SA = 6a^2$$

(Surface area)

$$\text{diag} = a\sqrt{3}$$

Cuboid

$$V \rightarrow l \times b \times h$$

$$SA = 2(lb + bh + hl)$$

$$\text{diag} = \sqrt{l^2 + b^2 + h^2}$$

Cylinder

$$V = \pi r^2 h$$

$$CSA = 2\pi r h$$

$$TSA = 2\pi r h + 2\pi r^2$$

$$2\pi r (h + r)$$

Cone

$$V = \frac{1}{3} \pi r^2 h$$

$$CSA = \pi r l$$

$$TSA = \pi r l + \pi r^2$$

$$\pi r (l + r)$$

Sphere

$$V = \frac{4}{3} \pi r^3$$

$$SA = 4\pi r^2$$

Hemisphere

$$V = \frac{2}{3} \pi r^3$$

$$CSA = 2\pi r^2$$

$$TSA = 3\pi r^2$$

Frustum

$$V = \frac{1}{3} \pi h [R^2 + r^2 + Rr]$$

gate 2022

Formula sheet

i) Max. possible coal faces = $3m-2$

Min. faces available = m

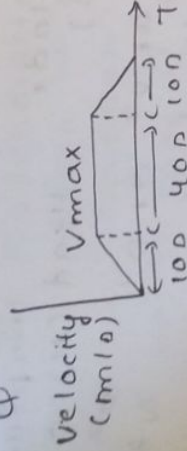
avg. no. of faces avail. = $2m-1$

$m = \text{no. of headings}$

ii) $FOS = \frac{\text{Strength}}{\text{load}}$

iii) $180^\circ = \pi \text{ rad}$

Φ



A mine winder cage travelling 450m from pit bottom to pit top is following a \approx

period duty cycle. V_{max} (cage) = ?

Sol.

Area of velocity time graph given distance

$$\frac{1}{2} \times 100 \times V_{max} + 40 \times V_{max}$$

$$+ \frac{1}{2} \times 100 \times V_{max} = 450 \text{ m}$$

$$V_{max} = \frac{450}{50} = 9 \text{ m/s}$$

Superelevation

(centrifugal ratio) $\frac{V^2}{gR}$ (on road)

$\frac{GV^2}{gR}$ (on railway)

$V = \text{train velocity}$
 $R = \text{radius of curve (m)}$

$g = \text{acc. due to gravity}$

$G = \text{track gauge (dist. b/w centers of rails)}$

Centrifugal ratio / Impact factor
 = centrifugal

$$= \frac{F}{W} = \frac{mv^2}{r} \div \frac{mg}{r}$$

$$= \frac{v^2}{gr}$$

→ law related to

ϕ, P, N

Pump

i) $\phi \propto N$ or v or D^3

$\phi \propto D$ or N

$v =$ peripheral speed of blade tips (m/s)

(Dia. of Impeller)

Head (H) \propto

ii) $Wg \propto N^2$ or ϕ^2 or v^2 or D^2

D^2 or N^2

iii) HP (req. to drive the fan)

BHP \propto

$\propto N^3$ or v^3 or ϕ^3 or D^5

D^3 or

$N =$ rpm of fan / impeller

N^3

Motive Column:-

$$H = \frac{NVP}{Pd \cdot g} \quad (K)$$

$$H = \frac{P_d - P_u}{P_d} \times D$$

$$H = \frac{T_u - T_d}{T_u} \times D$$

$$\% \text{ Utilization} = \frac{\text{Total hto of actual work}}{\text{Total available hto of work}} \times 100$$

→ Properties of Eigen values

$$|A - \lambda I| = 0$$

In diagonal matrix,

Eigen values are leading diag. elements

★ → $|A| = \text{Product of E.V.}$

$$\text{Trace} = \sum (\lambda)$$

→ Skew sym. matrix (odd order)

$$|A| = 0 \text{ (Singular)}$$

at least 1 E.V. = 0

→ E.V. / characteristic roots / latent roots → sol. of characteristic equation

→ In case of triangular matrix, leading diagonal elements are eigen values

$$\text{Q } A = \begin{bmatrix} 3 & 2 & 5 \\ 2 & 2 & 1 \\ 1 & 5 & 4 \end{bmatrix}$$

$$\begin{aligned} \text{Product of EV} &= 3(8-5) - 2(8-1) + 5(10-2) \\ &= 3(3) - 2(7) + 5(8) \\ &= 9 - 14 + 40 = 35 \end{aligned}$$

⇒ Range kutta method (4th order)

Given ODE

$$\frac{dy}{dx} = f(x, y)$$

$$y(x_0) = y_0$$

To find $y(x_1)$

$$\text{RKM} \rightarrow y_{m+1} = y_m + \frac{1}{6} [k_1 + 2k_2 + 2k_3 + k_4]$$

$$K_1 = hf(x_n, y_n)$$

$$K_2 = hf\left(x_n + \frac{h}{2}, y_n + \frac{K_1}{2}\right)$$

$$K_3 = hf\left(x_n + \frac{h}{2}, y_n + \frac{K_2}{2}\right)$$

$$K_4 = hf(x_n + h, y_n + K_3)$$

$$x_1 = x_0 + h$$

$$x_2 = x_1 + h$$

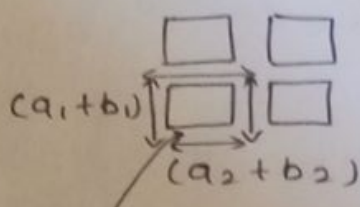
→ Elastic Potential

$$\text{energy of spring} = \frac{1}{2} kx^2$$

\downarrow
 Spring stiffness (N/m)

→ Percentage of extraction

$$= \frac{\text{Vol. of coal extraction during development}}{\text{Total in situ coal}}$$



$$R = \frac{(a_1 + b_1)(a_2 + b_2) - a_1 a_2}{(a_1 + b_1)(a_2 + b_2)}$$

$$R = 1 - \frac{a^2}{(a+b)^2}$$

Tributary area

$$= \frac{(a_1 + b_1)(a_2 + b_2) - a_1 a_2}{(a_1 + b_1)(a_2 + b_2)}$$

⇒ load acting on pillar :-

$$P = \frac{\gamma D}{1-R} \text{ or } \gamma D \frac{(a+b)^2}{a^2}$$

Percentage of extraction

D = Depth of pillar from surface

a = length & breadth of pillar

b = width of galleries

γ = weight/unit vol. of superincumbent rock

Strength of pillar :-

$$S = k \frac{W^\alpha}{L^\beta}$$

$\alpha = 0.46$
 $\beta = 0.66$

$1 \text{ lb/in}^2 = 0.0703 \text{ kg/cm}^2$
 $1 \text{ m} = 3.281 \text{ ft}$

1320 lb/in^2
 $W =$ Width of pillar (ft)
 $L =$ Height of pillar (ft)

→ FOS = $\frac{\text{Strength of pillar (S)}}{\text{load acting on pillar (P)}}$

Rock Mechanics

$$\gamma_d = \frac{\gamma_b}{1+m} \rightarrow \text{bulk unit weight}$$

\downarrow
 Dry unit weight
 $m \rightarrow$ moisture content

→ $RMR = 9 \ln(Q) + 44$

→ Sp. gravity = $\frac{w}{w-s} \rightarrow$ weight in air
 $w-s \rightarrow$ weight when suspended in water

\downarrow
 Rock mass quality

→ $n = \frac{e}{1+e}$ (Porosity) (void ratio)

→ $P_d = \frac{G_r P_w}{1+e} = (1-n) G_r P_w \left(\frac{M_{\text{solid}}}{V} \right)$

$\gamma_d = \frac{G_r \gamma_w}{1+e} \left(\frac{w_{\text{solid}}}{V} \right)$

$P_{\text{saturated}} = \frac{G_r + e}{1+e} P_w$

$\gamma_{\text{sat}} = \frac{G_r + e}{1+e} \gamma_w$ } density / unit weight of water

★ Simpson's 1/3 rule

$x_0 + nh$

$$\int_{x_0}^{1.5} f(x) dx = \frac{h}{3} \left[(y_0 + y_m) + 4(y_1 + y_3 + y_5 + \dots) + 2(y_2 + y_4 + y_6 + \dots) \right]$$

Q $\int_{0.5}^{1.5} \frac{dx}{x}$ using Simpson's rule with 3 point function exceeds exact value by

Point function:-

$x_0 \rightarrow y_0$

$x_1 \rightarrow y_1$

$x_2 \rightarrow y_2$

Sub interval = 2

↓
even

(Simpson's 1/3 rule)

exact value

1.5

$$I = \int_{0.5}^{1.5} \frac{dx}{x} = (\ln(x))_{0.5}^{1.5} = 1.0986$$

$y = \frac{1}{x}$

$x \quad 0.5 \quad 1 \quad 1.5$

$y \quad 2 \quad 1 \quad 2/3$

$y_0 \quad y_1 \quad y_2$

$$= \frac{0.5}{3} \left[(2.66) + 4(1) \right]$$

$= 1.11$

$= 0.0114 \text{ Ans}$

Q $I = \int_0^4 \sqrt{x} dx$ with 2 sub intervals $y = \sqrt{x}$

$x \quad 0 \quad 2 \quad 4$

$y \quad 0 \quad 1.414 \quad 2$

$y_0 \quad y_1 \quad y_2$

$$= \frac{2}{3} \left[(2) + 4(1.414) \right]$$

$= 5.104$

Queuing theory

M/M/1 Queuing system

$$\rho = \frac{\pi}{\mu} \rightarrow \text{arrival rate}$$

$$\mu \rightarrow \text{service rate}$$

Traffic density (proportion of time the server is busy)

$$P_0 =$$

(Prob. of 0 units in the system
(service unit is idle))

$$1 - \frac{\pi}{\mu}$$

Prob. of more than k units in the system

$$P_{n > k} = \left(\frac{\pi}{\mu}\right)^k$$

W_s (expected waiting time / customer in the system)

$$= \frac{1}{\mu - \pi}$$

W_q (exp. waiting time / customer in the queue)

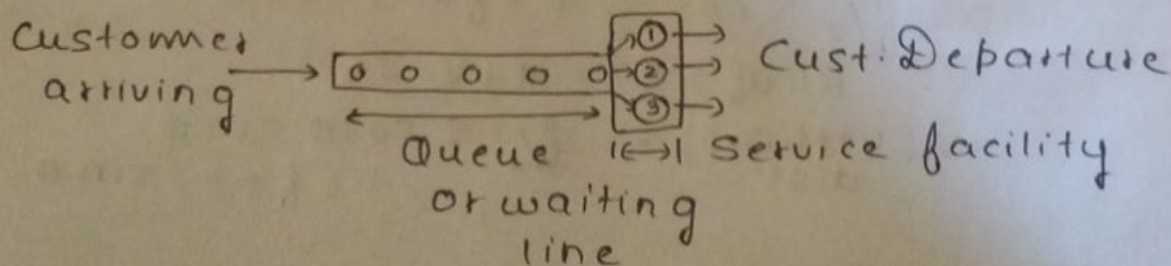
$$= \frac{\pi}{\mu(\mu - \pi)}$$

L_s (expected no. of customers in the system / length of system)

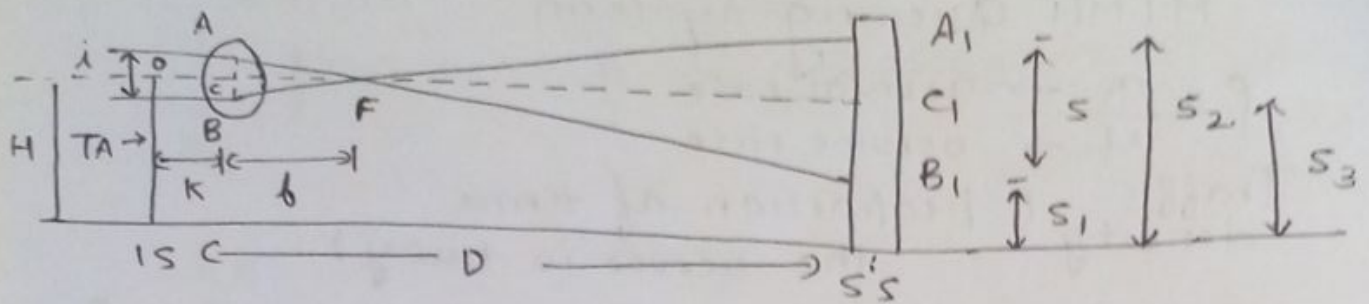
$$= \pi \cdot W_s = \frac{\pi}{\mu - \pi}$$

$$L_q = \pi \cdot W_q = \frac{\pi^2}{\mu(\mu - \pi)}$$

← system →



Tacheometric Surveying



f = focal length of object glass
 i = dist. b/w upper & lower stadia hairs

s = staff intercept ($s_2 - s_1$)

D = horizontal dist. b/w IS & SS

s_3 = axial hair reading

k = Dist. of trunnion axis from object glass

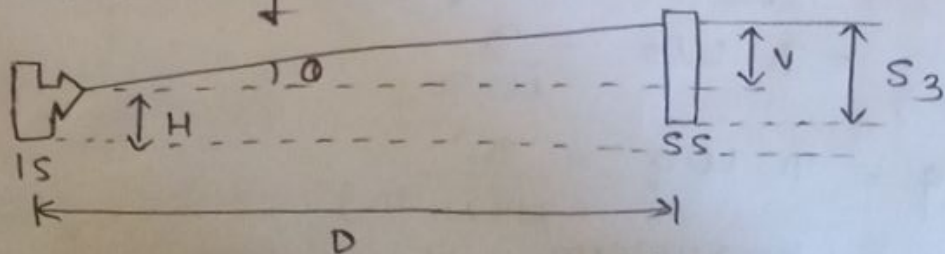
$$D = \frac{f}{i} s + (f+k)$$

f/i = multiplying constant = 100

$(f+k)$ = additive constant = 0 (for anallatic lens)

$$RL \text{ of } SS = HI - s_3$$

i) when line of sight is inclined to the horizontal and the staff is held vertically



$$D = \frac{f}{i} s \cos^2 \theta + (f+k) \cos \theta$$

$$RL \text{ of } SS = H + v - s_3$$

$$v \text{ (vertical dist.)} = \frac{f}{i} s \cos \theta \sin \theta + (f+k) \sin \theta$$

1000 SG

Concentration of sand
by weight (%)

$$= \frac{0.91V}{0.91V + 0.65V} \times 100$$

Imp

=

58.33% And

★ Conversions

$$1 \text{ Bar} = 10^5 \text{ Pa}$$

$$1 \text{ mm Hg} = 9.81 \text{ Pa}$$

$$1000 \text{ lit} = 1 \text{ m}^3$$

$$1 \text{ mm Hg} = 133.32 \text{ Pa}$$

$$1 \text{ Gallon} = 0.00379 \text{ m}^3$$

$$1 \text{ Barcy} = 9.86 \times 10^{-9} \text{ cm}^2$$

Standard

$$\text{Pressure} = 1.013 \times 10^5 \text{ N/m}^2$$

atmospheric

1 Weisbach/

$$1 \text{ Kilomurg} = 9.81 \text{ N s}^2 \text{ m}^{-8}$$

Match factor = $\frac{\text{Truck arrival rate}}{\text{loader service rate}}$
(Truck shovel comb.)

① On an old plan of scale 1:1000, lead hold area of a mine is now measured as 802 cm^2 using a planimeter. The plan is now being used to construct

$$\frac{d}{dx}(e^x) = e^x$$

$$\frac{d}{dx}(a^x) = (\ln a) a^x$$

$$\frac{d}{dx}(\sin^{-1}x) = \frac{1}{\sqrt{1-x^2}}$$

$$\frac{d}{dx}(\tan^{-1}x) = \frac{1}{1+x^2}$$

$$\frac{d}{dx}(\sec^{-1}x) = \frac{1}{|x|\sqrt{x^2-1}}$$

$$\frac{d}{dx}(uv)$$

$$= u \frac{dv}{dx} + v \frac{du}{dx}$$

$$\frac{d}{dx}\left(\frac{u}{v}\right)$$

$$= \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$$

Integration

$$\int x^m dx = \frac{x^{m+1}}{m+1} + c \quad (m \neq -1)$$

$$\int \sin x dx = -\cos x + c$$

$$\int \cos x dx = \sin x + c$$

$$\int \sec^2 x dx = \tan x + c$$

$$\int \csc^2 x dx = -\cot x + c$$

$$\int \sec x (\tan x) dx = \sec x + c$$

$$\int \csc x \cot x dx = -\csc x + c$$

$$\int \frac{1}{x} dx = \ln|x| + c$$

$$\int e^x dx = e^x + c$$

$$\int a^x dx = \frac{a^x}{\ln a} + c \quad (a > 0, a \neq 1)$$

$$\int \frac{1}{\sqrt{1-x^2}} dx = \sin^{-1}x + c$$

$$\int \frac{1}{1+x^2} dx = \tan^{-1}x + c$$

$$\int \frac{1}{|x|\sqrt{x^2-1}} dx = \sec^{-1}x + c$$

A.P.

Sum of first
n terms

$$= \frac{n}{2} [2a + (n-1)d]$$

n = no. of
terms

a = first term

d = common
difference

General form (AP)

$a, a+d, a+2d, \dots$

→ n^{th} term of AP series

$$T_n = a + (n-1)d$$

$d = \text{common diff.}$

$n = n^{\text{th}}$ term

→ If last term l is given, sum of n terms → $S_n = \frac{n}{2}(a+l)$

→ Sum of first n natural numbers
 $n = \text{no. of natural numbers}$ $= \frac{n(n+1)}{2}$

→ Sum of squares of first n natural no.
 $= \frac{n(n+1)(2n+1)}{6}$

→ Sum of first n odd no. $= n^2$

→ Sum of first n even numbers $= n(n+1)$

→ No. of terms in AP $n = \frac{(l-a)}{d} + 1$
 $l = \text{last term}$
 $a = \text{first term}$
 $d = \text{common diff.}$

→ If a, b, c is given in an AP series
 $b = \frac{a+c}{2}, b-a = c-b$

GP n^{th} term $T_n = ar^{n-1}$ $r = \text{common ratio}$

a, ar, ar^2, \dots

$2 \quad 4 \quad 8 \quad 16 \quad 32 \quad r=2$

→ S_n (sum of n terms)
 $= \frac{a(r^n - 1)}{r - 1}$

a, b, c

$$b^2 = ac$$

$$b = \sqrt{ac}$$

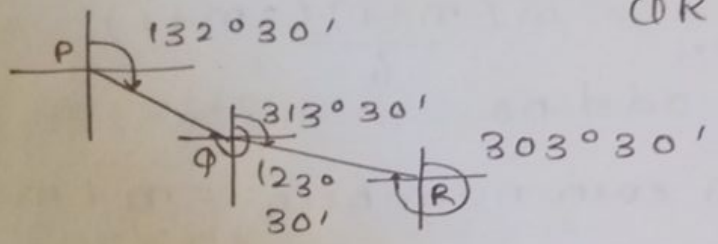
→ Infinite GP (S_{∞}) $= \frac{a}{1-r}$

Line	FB	BB
PQ	132°30'	313°30'
QR	123°30'	303°30'
RS	182°30'	2°15'
ST	288°45'	108°0'

Stations free from local attraction

Concept

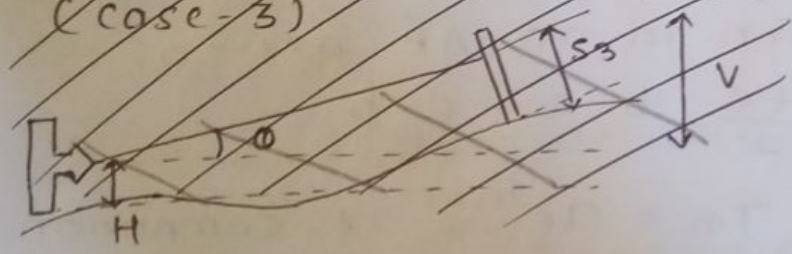
If the difference b/w FB & BB of a line is 180°, the two end stations of that line are free from local attraction



$$\begin{aligned} \text{QR} &= 303^\circ 30' - 123^\circ 30' \\ &= 180^\circ \end{aligned}$$

Q & R are free from local attraction

~~Tacheometric Surveying (Case-3)~~



Aerial Photogrammetry

$$\text{Scale} = \frac{\text{Photo dist.}}{\text{ground dist.}}$$

$$\frac{ab}{AB} = \frac{b}{H-h}$$

Scale of photograph /

Avg. photo scale

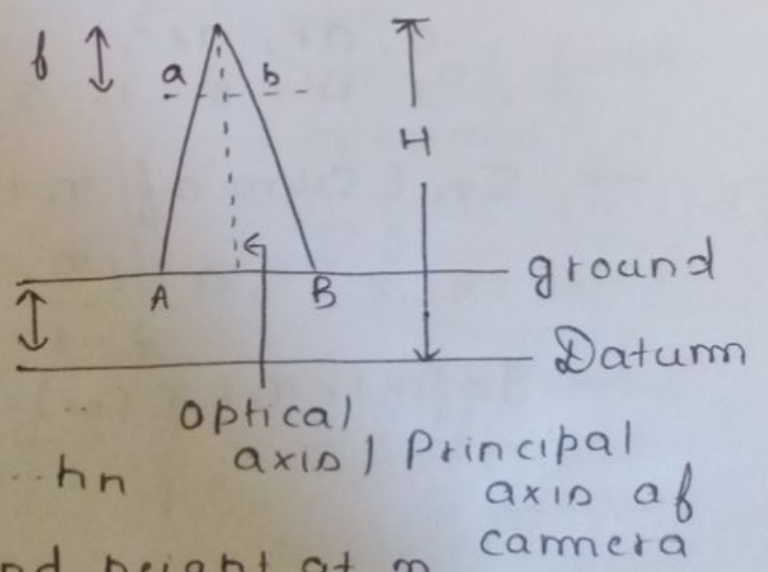
(depends on ground elevation)

$$= \frac{b}{H-h_{av}}$$

avg. elevation of ground =

$$\frac{h_1 + h_2 + \dots + h_n}{n}$$

n = ground height at n no. of points



No. of Photographs

$$\text{No. of Photos} = \frac{\text{A}_{\text{ground}}}{\text{Non overlapping area of photo}}$$

Ex:-

Scale of Photograph = 1 cm \rightarrow 100 m

Size photograph = 23 x 23 cm

$$A = 150 \text{ km}^2$$

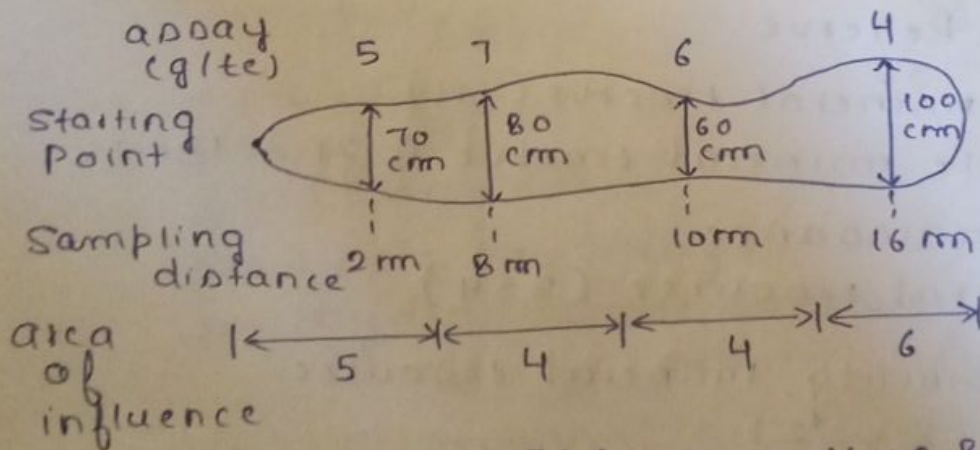
$$O_{\text{long.}} = 60\%$$

$$O_{\text{side}} = 30\%$$

$$N = \frac{150}{(1-0.6) \frac{100 \times 23}{1000} \times (1-0.3) \frac{100 \times 23}{1000}}$$
$$= \frac{150}{0.92 \times 1.61} = 101.269$$

Q The chip sampling data, spaced irregularly for a gold vein deposit

mean assay value (g/te) = ?



$$= \frac{5 \times 0.7 \times 5 + 4 \times 0.8 \times 7 + 4 \times 0.6 \times 6 + 6 \times 1 \times 4}{5 \times 0.7 + 4 \times 0.8 + 4 \times 0.6 + 6}$$

$$= 5.18 \text{ g/te}$$

→ Expected total error
(same error)

$$= \sqrt{e^2 + e^2} = \sqrt{2e^2} = e\sqrt{2}$$

→ Correction for curvature of earth

Correction is subtractive

$$0.0785 D^2$$

↓ Dist. b/w IS & SS

True staff reading = Observed staff reading - $0.0785 D^2$

→ Correction for refraction

corr. is additive

$$B \quad 0.0112 D^2$$

$$TSR = OSR + 0.0112 D^2$$

→ Combined correction = - corr. of curvature + corr. of refraction
 $= \frac{6D^2}{14R} \rightarrow$ Radius of earth
(subtractive)

→ Correlation Coefficient

r is the corr. coeff. It is always b/w $+1$ & -1

$+1 \rightarrow$ Points are on a perfect straight

times line with -ve slope

$+1 \rightarrow$ Points are on a perfect straight

line with +ve slope

→ coeff. of determination = r^2

X, Y → degree of relationship
(variables) → corr. coeff. r

→ Types of correlation
Perfect correlation → $r = 1$

+ve corr. → $X \uparrow, Y \uparrow$

-ve corr. → $X \uparrow, Y \downarrow$, $Y \uparrow, X \downarrow$

no corr. → No change in Y with X

→ Methods of Correlation

i) Coeff. of correlation (Karl Spearman's)

ii) Rank correlation

X	Y	$\bar{x} = \frac{\sum x_i}{n}$	n = no. of data points
x ₁	y ₁		
x ₂	y ₂	$\bar{y} = \frac{\sum y_i}{n}$	
⋮	⋮		
x _n	y _n		

$$r = \frac{\sum (x - \bar{x})(y - \bar{y})}{\sqrt{\sum (x - \bar{x})^2} \sqrt{\sum (y - \bar{y})^2}}$$

$$r = \frac{n \sum uv - \sum u \times \sum v}{\sqrt{n \sum u^2 - (\sum u)^2} \sqrt{n \sum v^2 - (\sum v)^2}}$$

u = x - A A = assumed mean for x values
 v = y - B B = assumed mean for y values

assumed mean = no. closest to arithmetic mean

→ Correlation Coeff.

$$= \frac{E(xy) - (E(x) \times E(y))}{\sqrt{(E(x^2) - (E(x))^2)(E(y^2) - (E(y))^2)}}$$

⇒ Relative humidity = $\frac{\text{mass of water vapour / m}^3 \text{ of air}}{\text{mass of water vapour required to saturate 1 m}^3 \text{ of air}}$

⇒ Reynold's number

Re ≤ 2000 (laminar flow of air)

Re > 4000 (turbulent air flow)

2000 < Re < 4000 (Transitional flow of air)

Mean value / expected value

$$= \sum x f(x) p(x)$$

Mean sq. value = $\sum x^2 f(x) p(x)$

UNFC (United Nations Framework classification)

UNFC consist of following 3 axis :-

- i) Geological assessment
- ii) Feasibility assessment
- iii) economic viability

→ highest category of resources under UNFC system will have code (111) & lowest category code (334)

Total mineral resource

- (i) Measured mineral resource (331)
- (ii) Indicated mineral resource (332)
- (iii) Inferred mineral resource (333)

Mineral Reserve

- (i) Proved mineral reserve (111)
- (ii) Probable mineral reserve (121 & 122)
- (iii) Reconnaissance mineral resource (334)

Prefeasibility mineral resource (221 & 222)

Feasibility mineral resource (211)

- k = coeff. of thermal conductivity
- c = Specific heat of rock sample
- ρ = density of rock sample

$$\text{Thermal diffusivity} = \frac{k}{\rho c}$$

$$\rightarrow \text{Coeff. of variation} = \frac{\sigma}{\mu}$$

$$\text{Sample st. deviation} = \sqrt{\frac{\sum (x - \mu)^2}{n-1}}$$

$$\rightarrow \frac{\sigma_H}{\sigma_v} = \frac{v}{1-v}$$

- Swell factor = Swell factor of soil is the amount of volume increase from the undisturbed to the excavated state due to air pockets created

Rock mechanics

$$\rightarrow \text{Bulking factor of rock} = \frac{\text{Vol. of rock after blasting}}{\text{Vol. of rock before blasting}}$$

(K)

$$\rightarrow \phi = kA \left(\frac{dh}{dL} \right)$$

↓ (Darcy's law)

Flow rate (m^3/day)

k = hydraulic conductivity (coeff. of permeability) (m/day)

A = cr. sectional area (m^2)

$\frac{dh}{dL}$ = hydraulic gradient

~~$$\rightarrow \text{Moisture content} = \frac{W_{\text{water}}}{W_{\text{solids}}} \times 100$$~~

~~$$\rightarrow \text{Void Ratio} = \frac{V_{\text{voids}}}{V_{\text{solids}}}$$~~

(e)

$$d \text{ (density)} = \frac{W_d \text{ (weight of solid)}}{V \cdot c}$$

→ Centrifugal tension in belt

$$T_c \text{ drive} = m v^2$$

Q An air receiver of a compressor having vol. 0.5 m^3 , supplies air for charging ANFO in drill holes. During charging process the absolute pressure of the air receiver falls from 900 to 700 kPa. Assuming the entire process is isothermal, the vol. of air supplied by the receiver at 100 kPa ambient pressure (m^3) is

Sol

Boyle's law

$V \propto \frac{1}{P}$ if temp. is constant

$$V_1 P_1 = V_2 P_2 = c$$

initial / final absolute pressure & volume

Charles's law

$V \propto$ absolute temp.

if pressure is constant

$$\frac{V_2}{V_1} = \frac{t_2}{t_1} = \frac{273 + c_1}{273 + c_2} = c$$

↓

absolute temp.

Graham's law of diffusion

$$R \propto \frac{1}{\sqrt{D}} \rightarrow \text{Relative densities of gases}$$

Relative rates
of diffusion
of gases

$$\frac{R_A}{R_B} = \sqrt{\frac{D_B}{D_A}}$$

$$\text{mmHg} = \text{kg/m}^2$$

As per Boyle's law

$$P_1 V_1 = P_2 V_2$$

let initial vol. be x

$$(0.5 - x) 900 = 700 \times 0.5 \\ = 0.111$$

Now at $P = 100 \text{ kPa}$

$$900 \times 0.111 = V \times 100$$

$$V = 1 \text{ m}^3 \text{ And}$$

Friction / koepe winding

$$\frac{T_1}{T_2} = e^{\mu \theta}$$

θ = angle of wrap

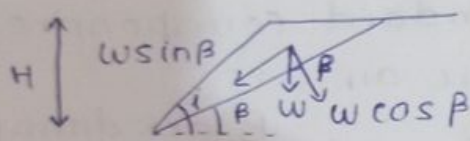
T_1 = Tension in the rope entering / leaving the wheel

μ = coeff. of friction
blw rope & wheel

Q A conveyor belt consumes 60 kW power while turning at a speed. Analyze

Determination of factor of safety of the slope

Case i) when there is no tension crack & water pressure



w = Weight of block
 c = cohesion
 ϕ = friction angle

β = angle of discontinuity from horizontal

A = Area of failure plane
 (Shear strength of sliding surface is expressed in terms of cohesion (c) & friction angle (ϕ))

Force tending to induce sliding = $w \sin \beta$

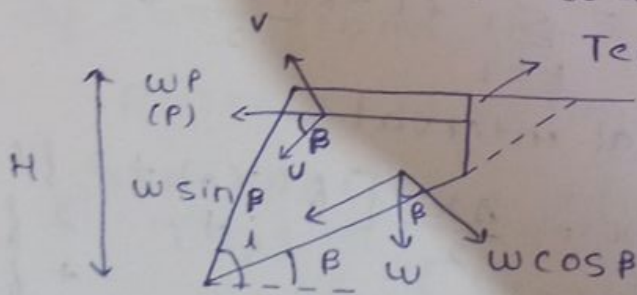
Force to resist sliding of the block =

$$w \cos \beta \cdot \tan \phi$$

$$FOS = \frac{\text{Force to resist sliding} + c \cdot A}{\text{Force tending to induce sliding}}$$

$$= \frac{w \cos \beta \tan \phi + cA}{w \sin \beta}$$

Case ii) Tension crack & water pressure present



Force tending to induce block sliding = $w \sin \beta + U$

$$FOS = \frac{c \cdot A + (w \cos \beta - v) \tan \phi}{w \sin \beta + U}$$

Water Pr. along sliding plane (U) = $P \cos \beta$

Water Pr. normal to the sliding plane

$(v) = P \sin \beta$
 Force resisting block sliding = $(w \cos \beta - v) \tan \phi + c \cdot A$

⇒ Absolute Weight Strength (AWS) :-
theoretical absolute energy available
based on ingredients of explosive
(MJ/kg of exp.)

Relative weight Strength :-

$$RWS_{exp} = \frac{AWS_{exp}}{AWS_{ANFO}} \times 100$$

Absolute bulk

Strength :-

Energy available in
unit vol. of explosive

$$ABS_{exp} \text{ (cal/cc)} = AWS_{exp} \times \rho_{exp}$$

Relative bulk strength :- $\frac{ABS_{exp} \times 100}{ABS_{ANFO}}$

⊕ Relative strength of an unknown explosive
is 1.5 with respect to ANFO.

Q Assignment Problem

$$\begin{aligned}
 &+ 100 \times 100 \times 8 \\
 &+ 200 \times 100 \times 12 \\
 = &120000 + 20000 \\
 &+ 25600 + 84000 \times 100 \\
 &\underline{800,000} \\
 &= 31.2\%
 \end{aligned}$$

T \ G	T ₁	T ₂	T ₃	T ₄
G ₁	6	10	5	4
G ₂	4	100	6	4
G ₃	6	9	6	2
G ₄	3	7	6	4

minimum cost of assignment = ?

Sol

1. Subtract the minimum value of each row from the entries of that row
2. Sub. the min. value of each column from the entries of that column

2	6	1	0
0	96	2	0
4	7	4	0
0	4	3	1

2	2	10	0
0	92	1	0
4	3	3	0
0	0	2	1

3. Row Scanning

→ Is there exactly 1 zero in that row?

if no, skip that row

if yes, mark a square around that 0 and draw a vertical line

passing through that 0

if all zeros are not covered,

do column scanning

4. if no. of square marked \neq
no. of rows
Identify minimum
value of undeleted
cell values

a) Add min. undeleted cell value at
the intersection points of
matrix

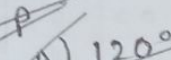
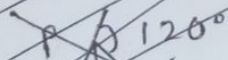
b) Subtract it from all
undeleted cell values

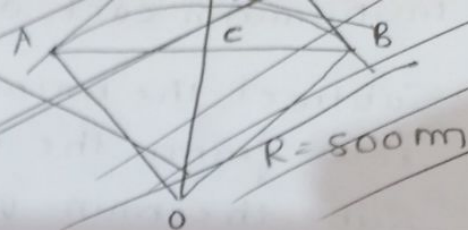
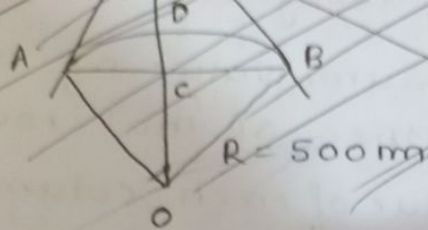
and do row column scanning again

$$= 5 + 4 + 2 + 7 = 18$$

★★

Q value of mid ordinate of curve ADB
(cm) = ?





Stress Distribution around circular excavation

Radial stress

$$\sigma_r = \frac{P}{2} \left[(1+k) \left[1 - \frac{a^2}{r^2} \right] - (1-k) \right]$$

Tangential stress

$$\sigma_\theta = \frac{P}{2} \left[(1+k) \left[1 + \frac{a^2}{r^2} \right] + (1-k) \left[1 - \frac{4a^2}{r^2} + \frac{3a^4}{r^4} \right] \cos 2\theta \right]$$

Shear stress

$$\sigma_{r\theta} = \frac{P}{2} \left[(1-k) \left[1 + \frac{3a^4}{r^4} \right] \cos 2\theta \right. \\ \left. \left[1 + \frac{2a^2}{r^2} - \frac{3a^4}{r^4} \right] \sin 2\theta \right]$$

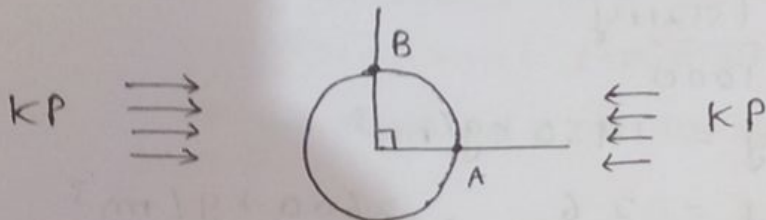
Stresses on the excavation boundary ($r=a$)

$$\sigma_r = 0$$

$$\sigma_\theta = P [(1+k) + 2(1-k) \cos 2\theta]$$

$$\sigma_{r\theta} = 0$$

$$\downarrow \downarrow \downarrow P$$



Boundary stresses (A)

$$\theta = 0$$

$$(\sigma_\theta)_A$$

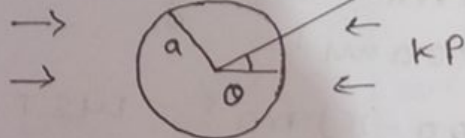
$$= P(3-k)$$

$$B \rightarrow \theta = \frac{\pi}{2}$$

$$(\sigma_\theta)_B = P(3k-1)$$

$$\uparrow \uparrow \uparrow \uparrow P$$

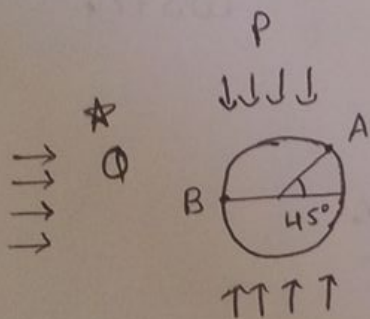
$$\downarrow \downarrow$$



For hydrostatic stress field ($k=1$)

$$\sigma_r = P \left[\left(1 - \frac{a^2}{r^2} \right) \right]$$

$$\sigma_\theta = P \left[\left(1 + \frac{a^2}{r^2} \right) \right]$$



$$(\sigma_\theta)_A = 3(\sigma_\theta)_B$$

$$\frac{P [(1+k) + 2(1-k) \cos 90]}{P [(1+k) + 2(1-k) \cos 360]} = 3$$

$$= \frac{1+k}{(1+k) + 2(1-k)} = 3$$

$$= \frac{1+k}{(1+k) + 2(1-k)}$$

$$= 1+k = 3(1+k+2-2k)$$

$$= 1+k = 3+3k+6-6k$$

$$= 1+k = 9-3k$$

$$= 4k = 8$$

$$k = 2$$

$$k = 2$$